



Νέες Τεχνολογίες στην Ανάλυση της Κίνησης

Διάλεξη 1

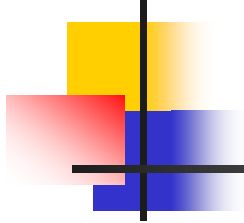
Σφάλμα – Ανάλυση χρόνου και συχνοτήτων –
Εξομάλυνση δεδομένων

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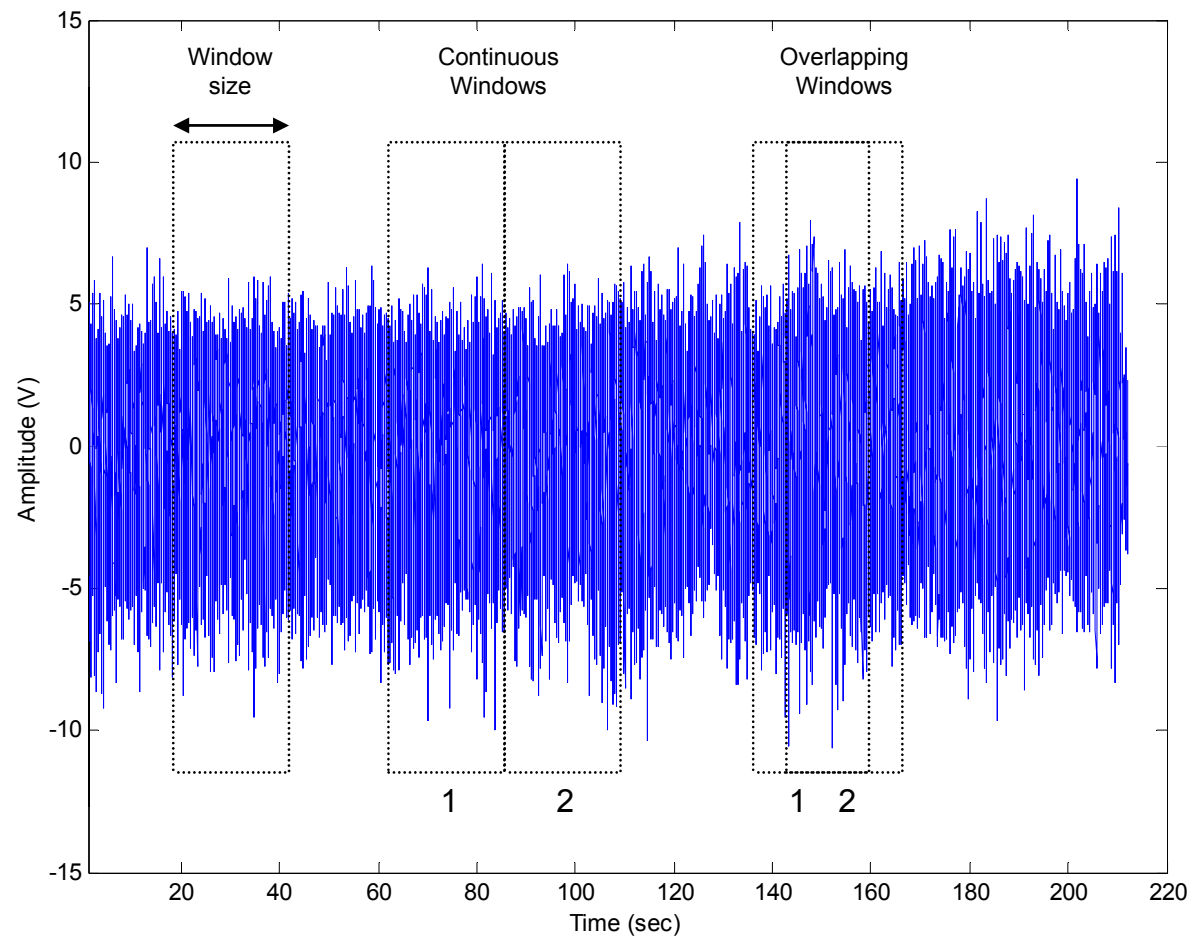
Presentation Outline

- Background – Problems
- Solutions
- Current / future research



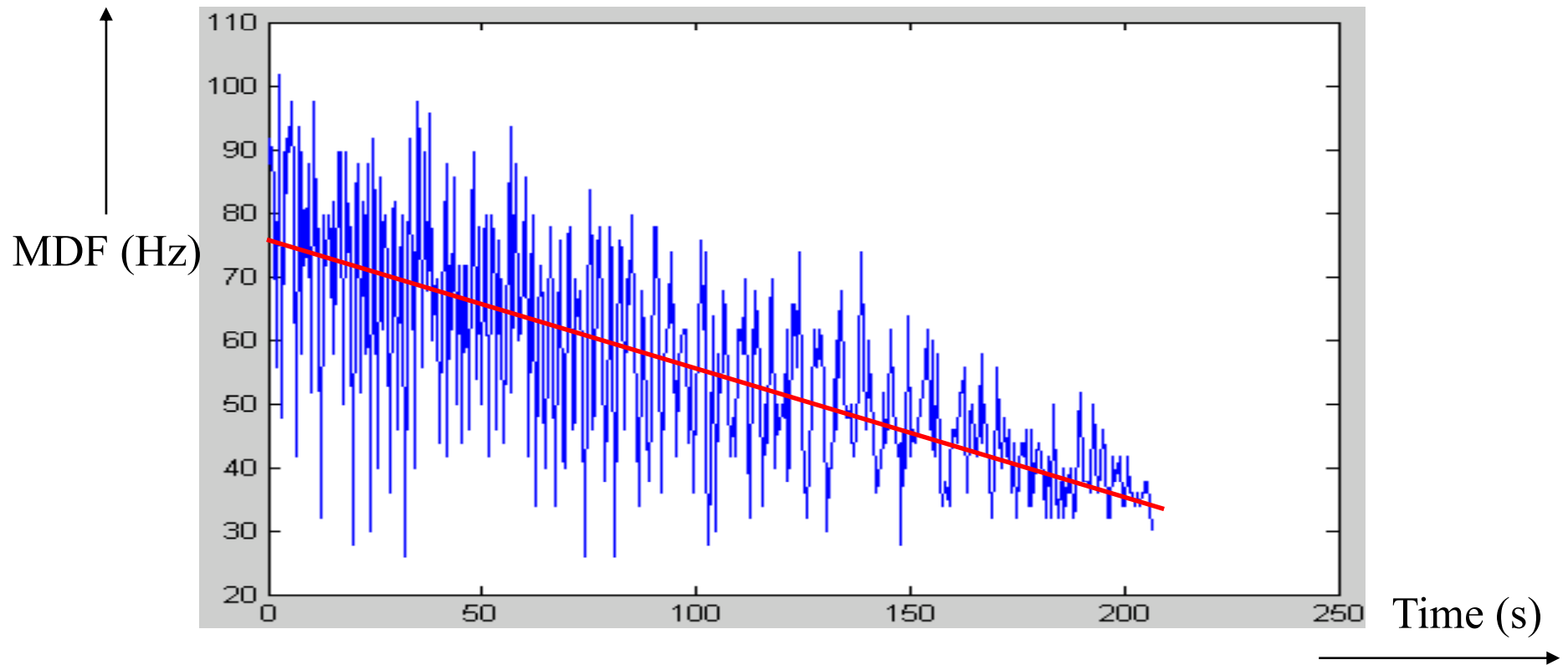


Signal analysis



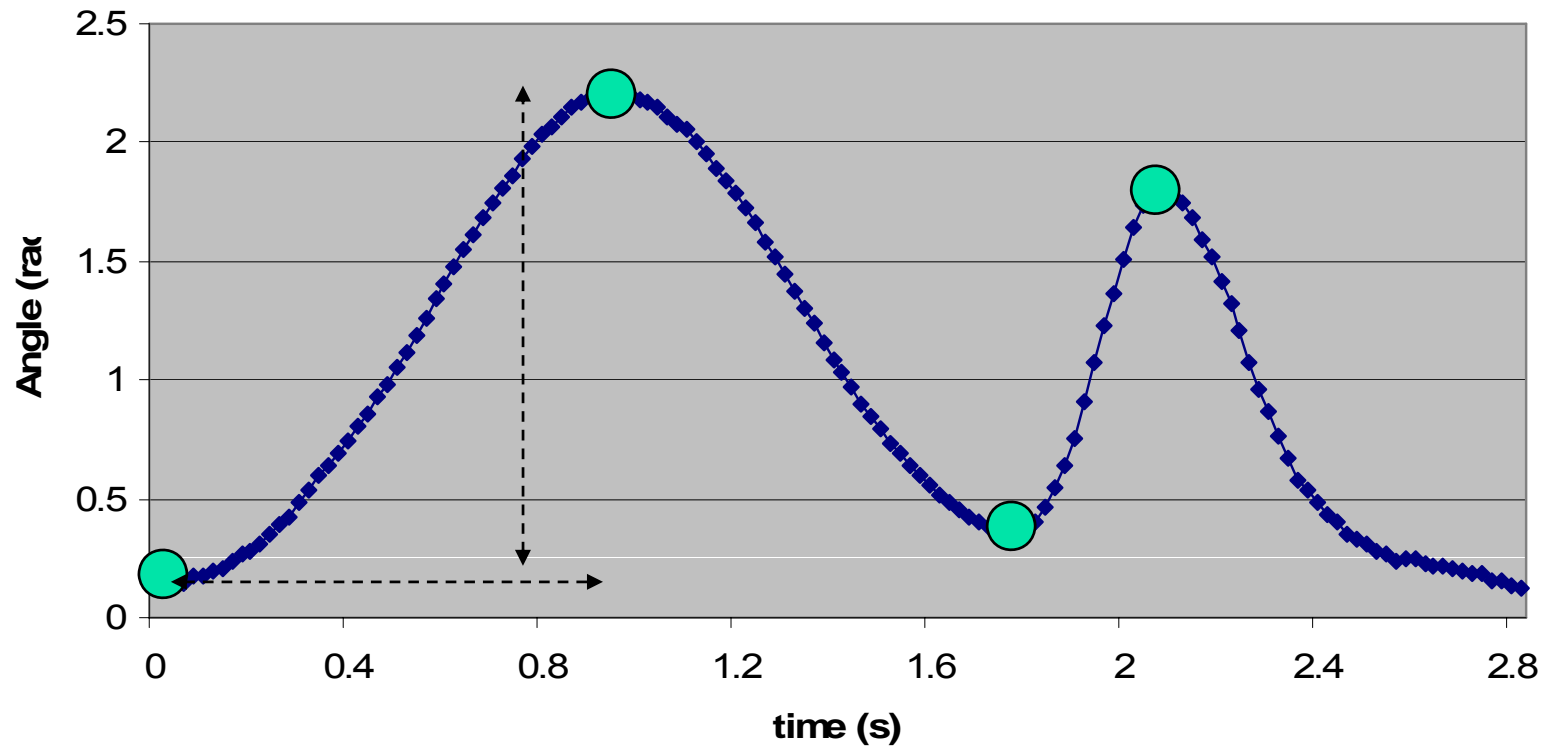


Signal analysis

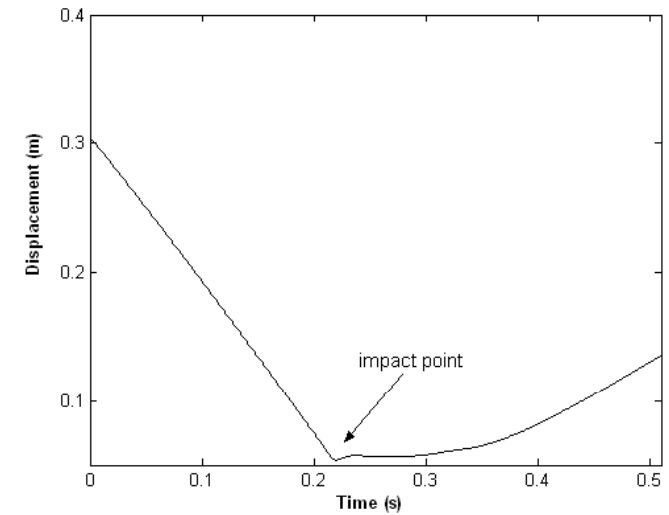
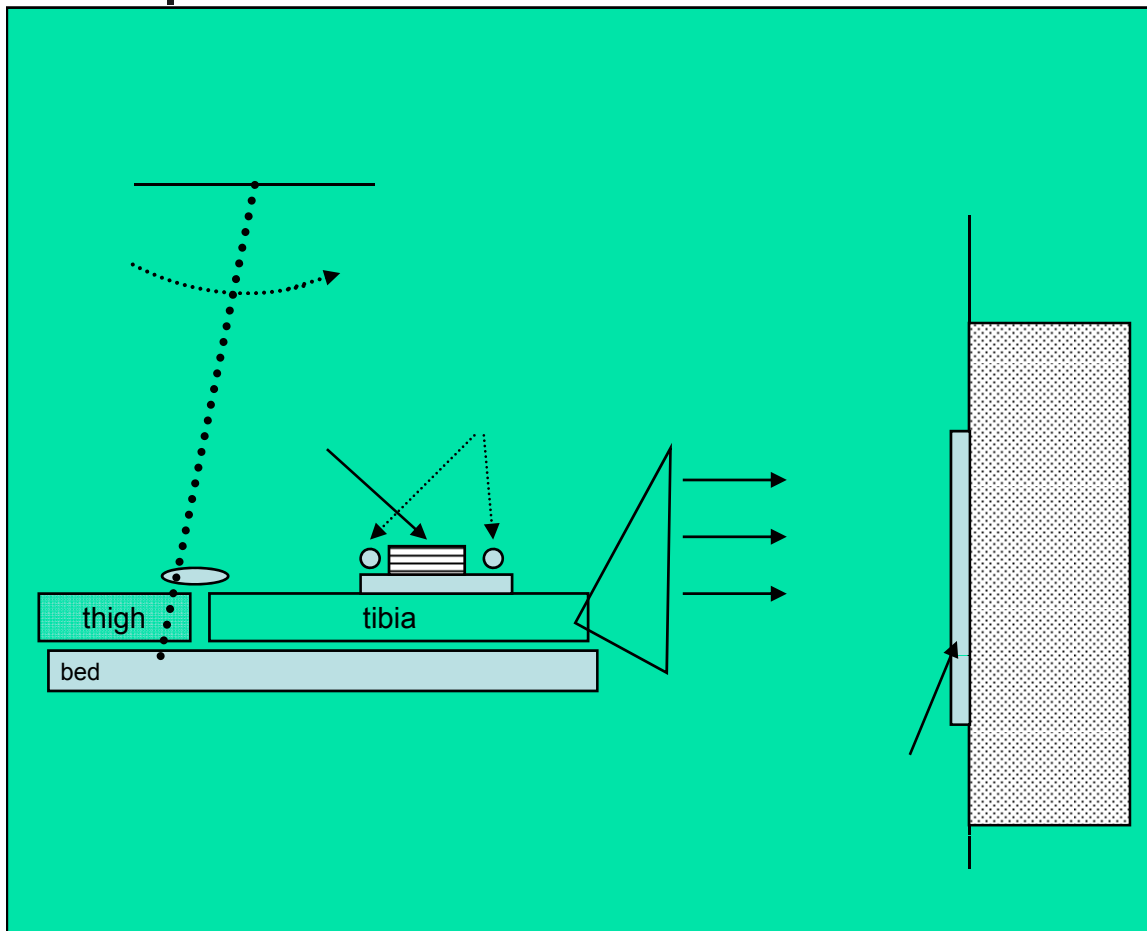




Signal analysis

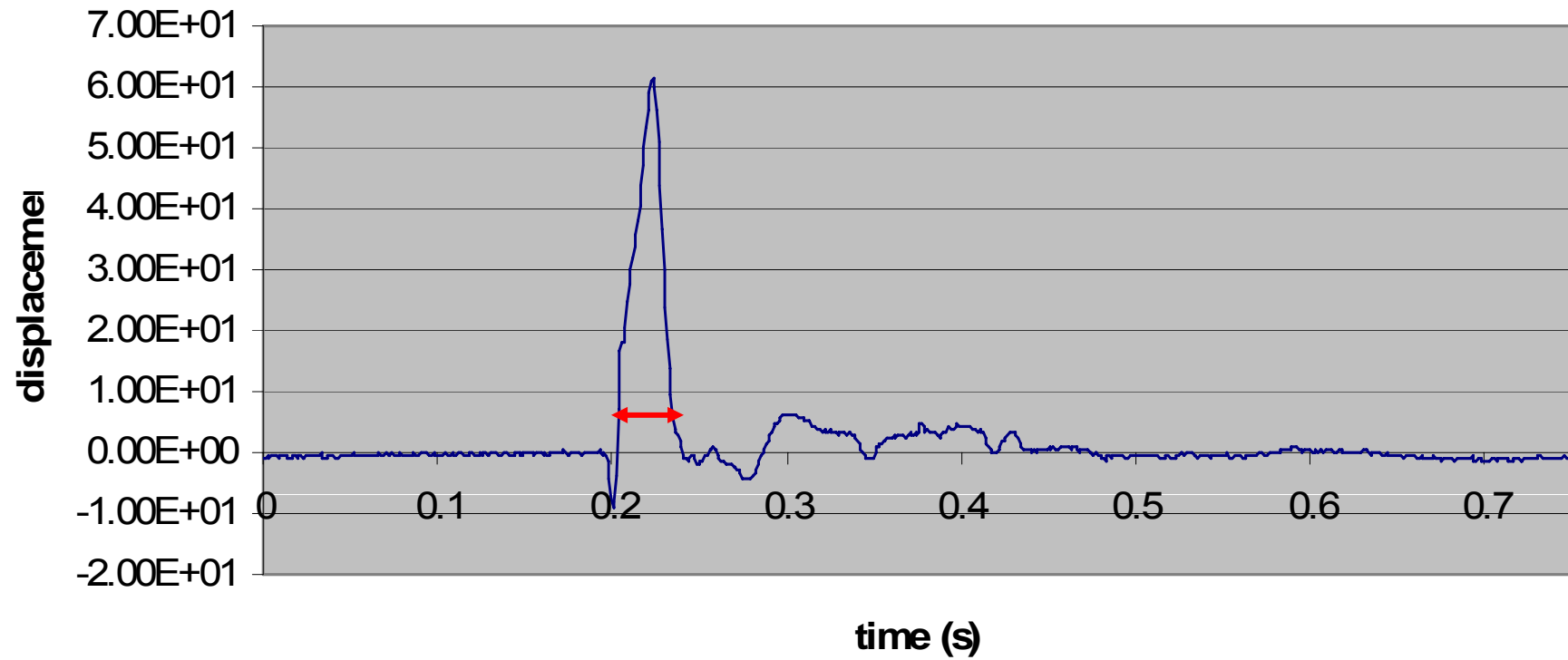


Signal analysis

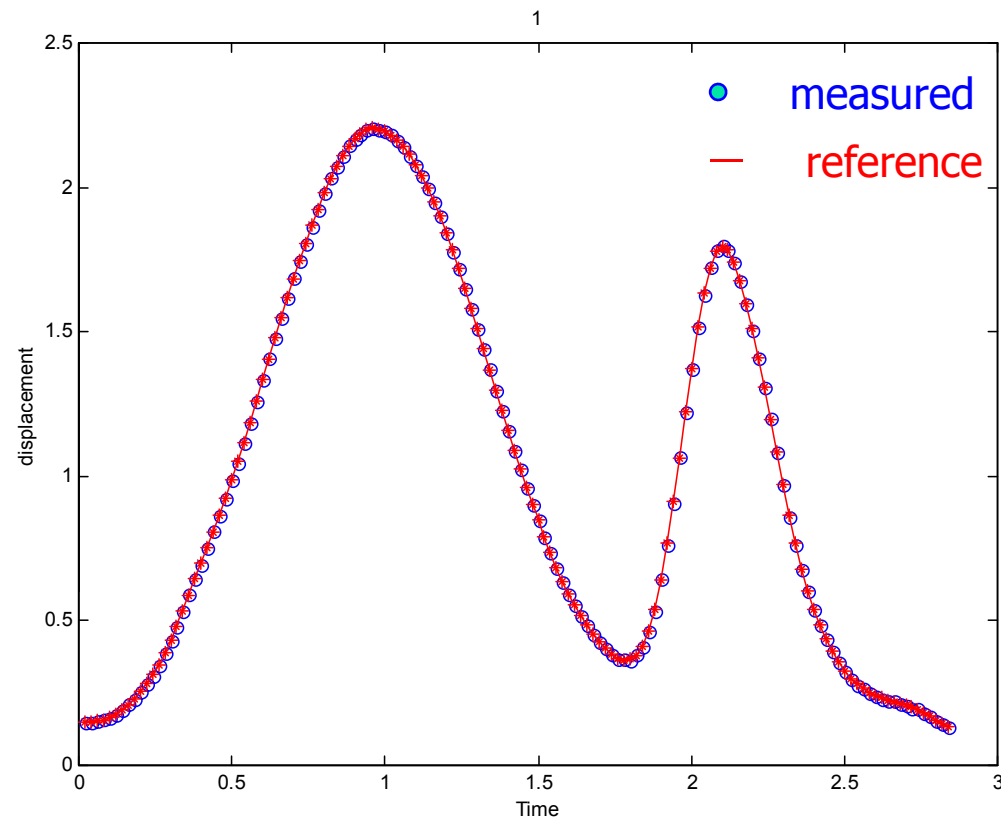


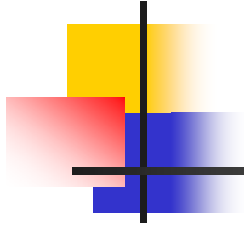


Signal analysis



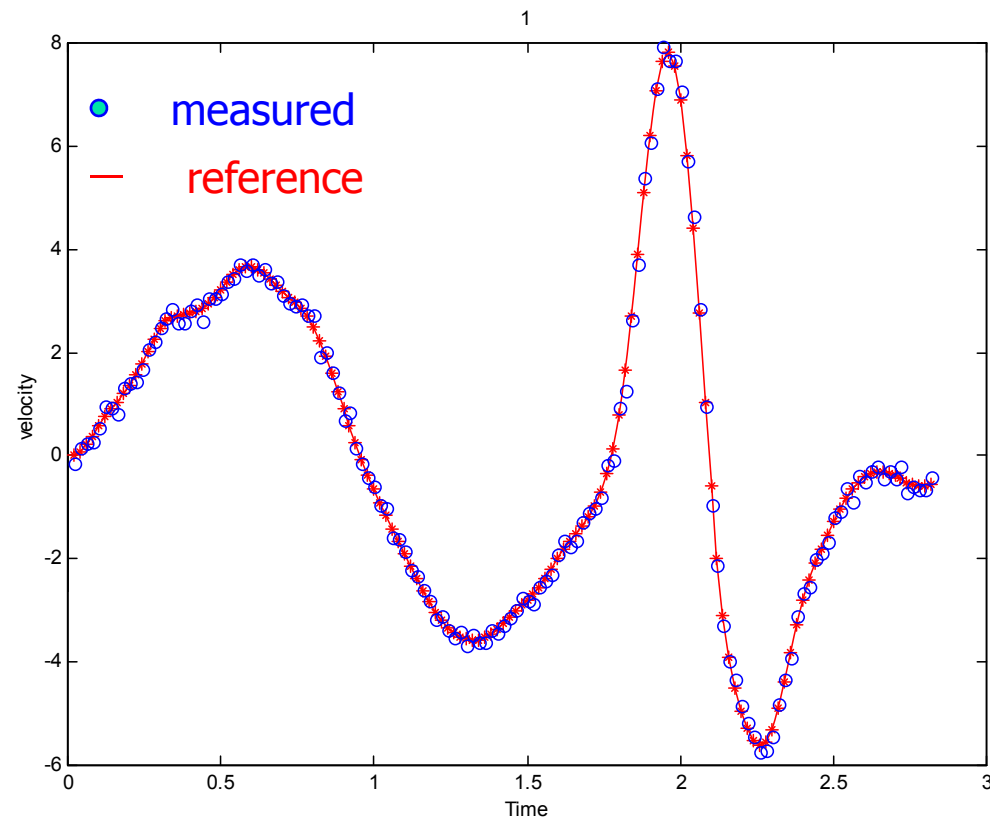
The effect of error : displacement



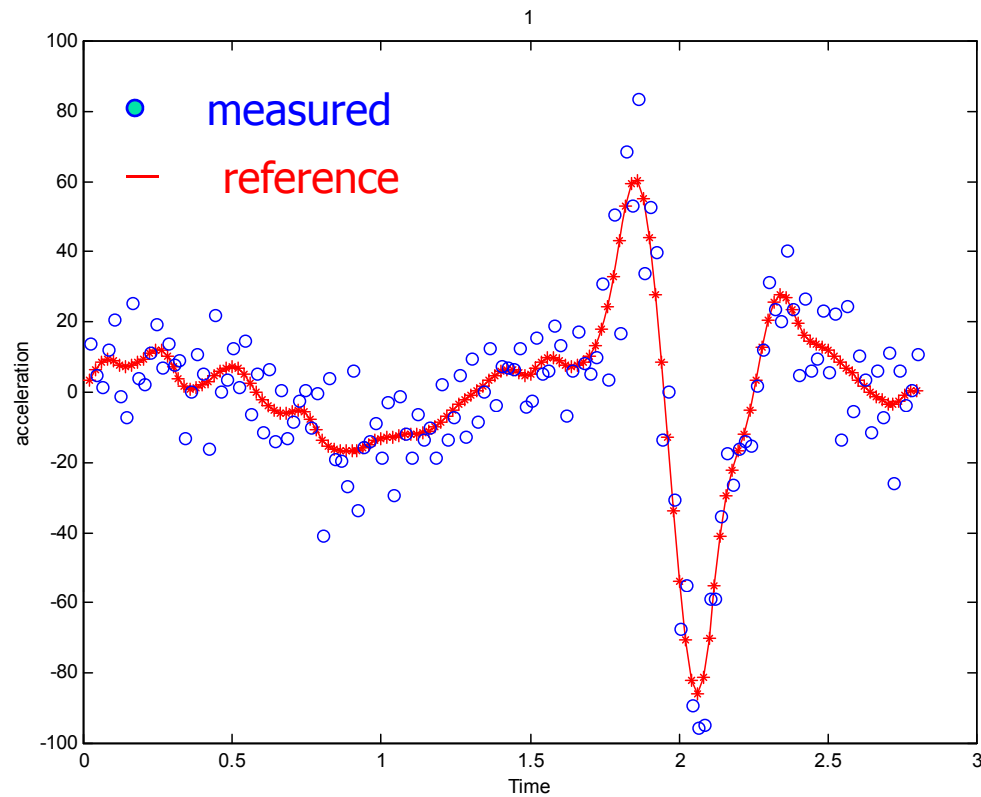


-
- Velocity = displacement / time
 - Velocity = DER(Displacement)
 - Acceleration = velocity / time
 - Acceleration = DER (Velocity) = DER_DER(Displacement)

The effect of error : velocity



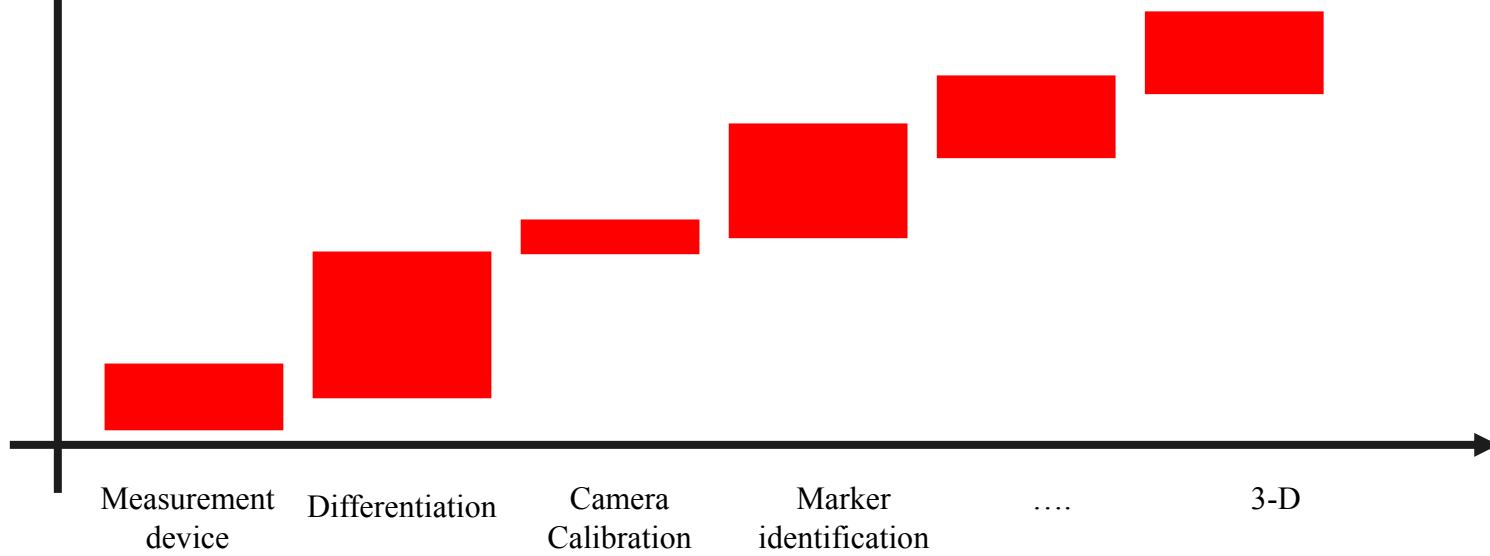
The effect of error : acceleration



Reference acceleration provided by Graeme Wood, 1997

Sources of error

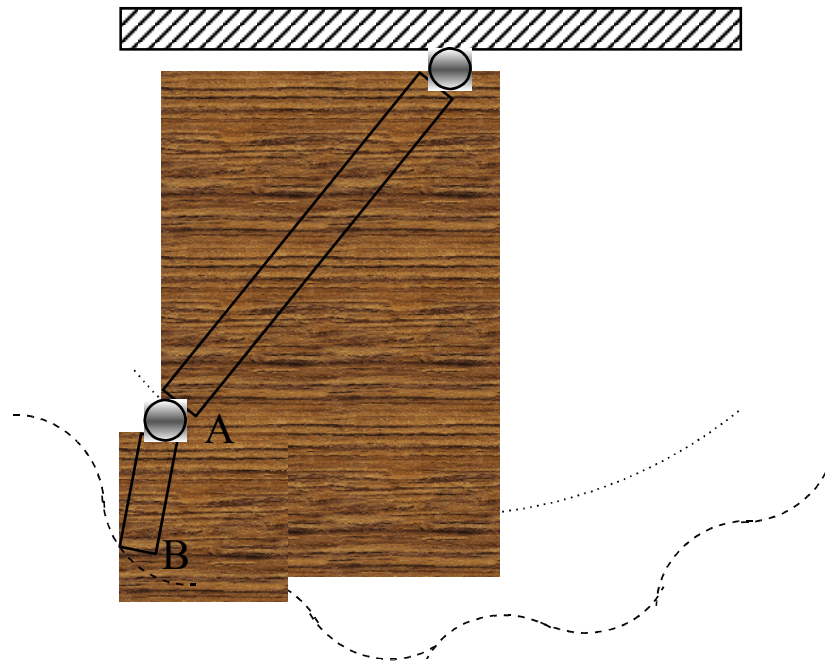
Error

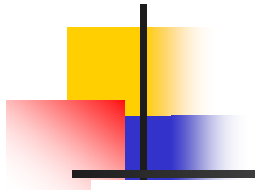




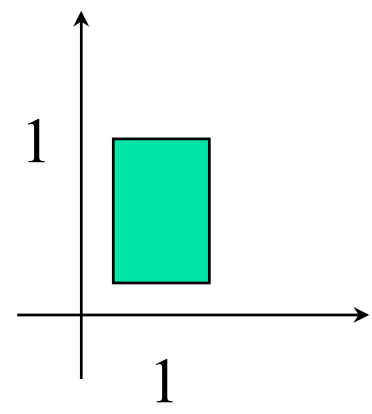
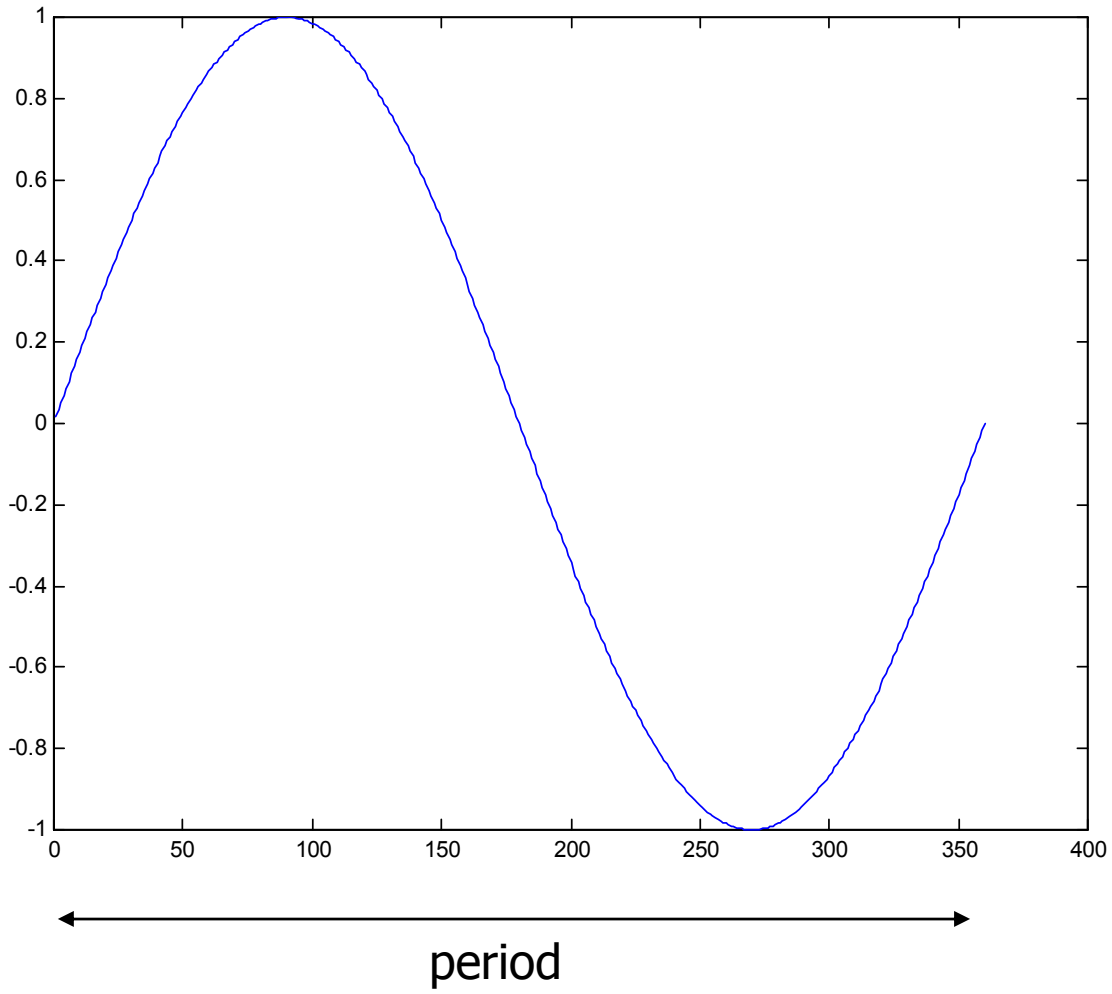
Why is this happening ?

- Frequency domain analysis



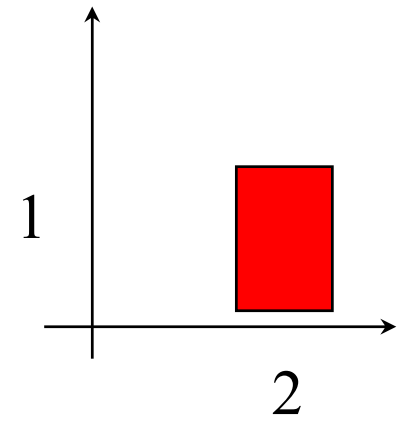
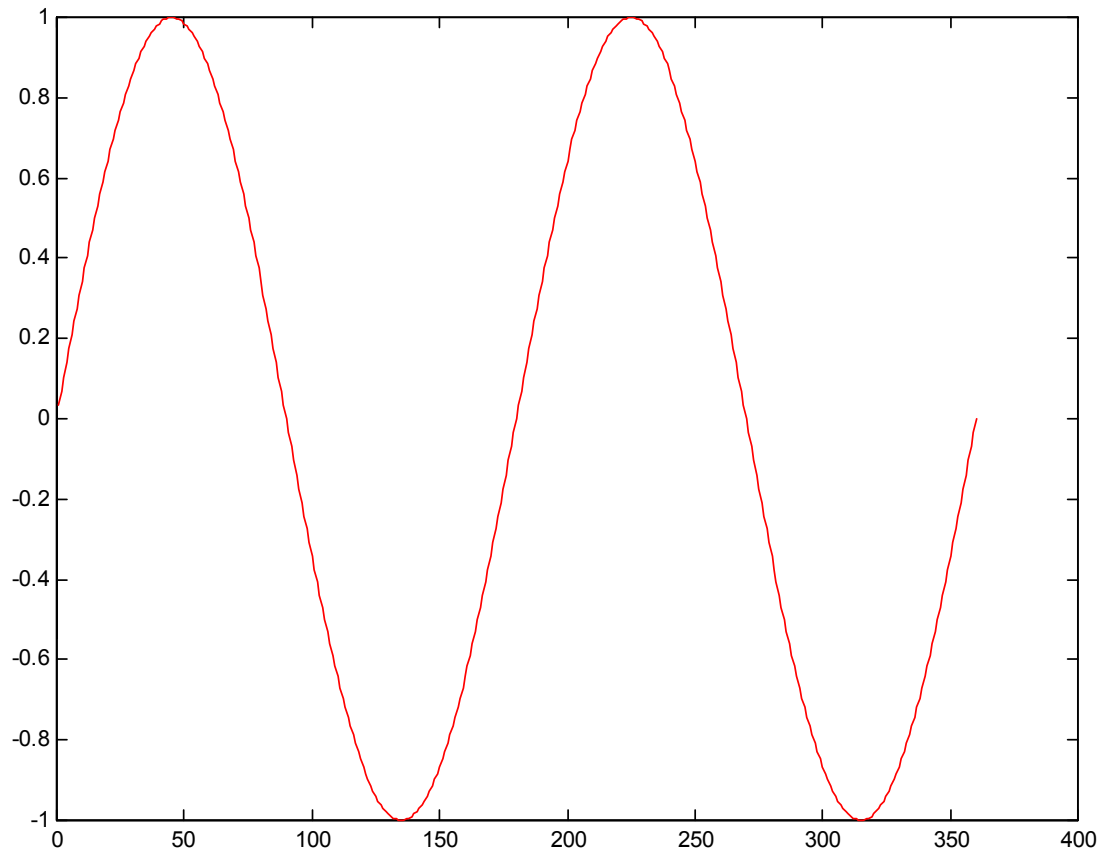


$$1 * \text{Sin}(1x)$$





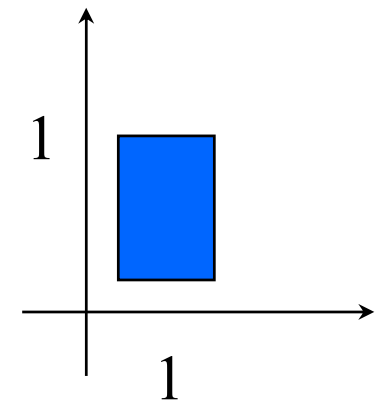
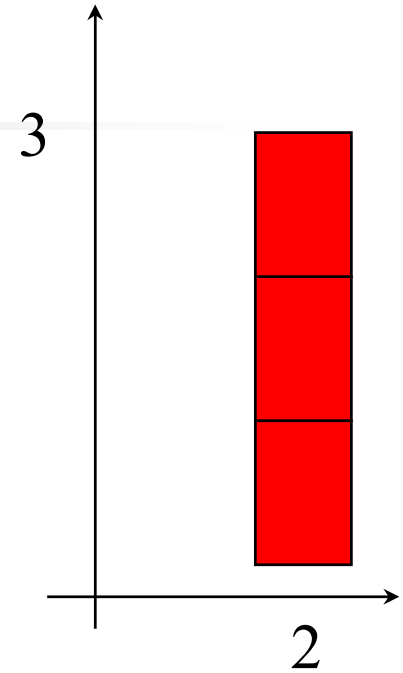
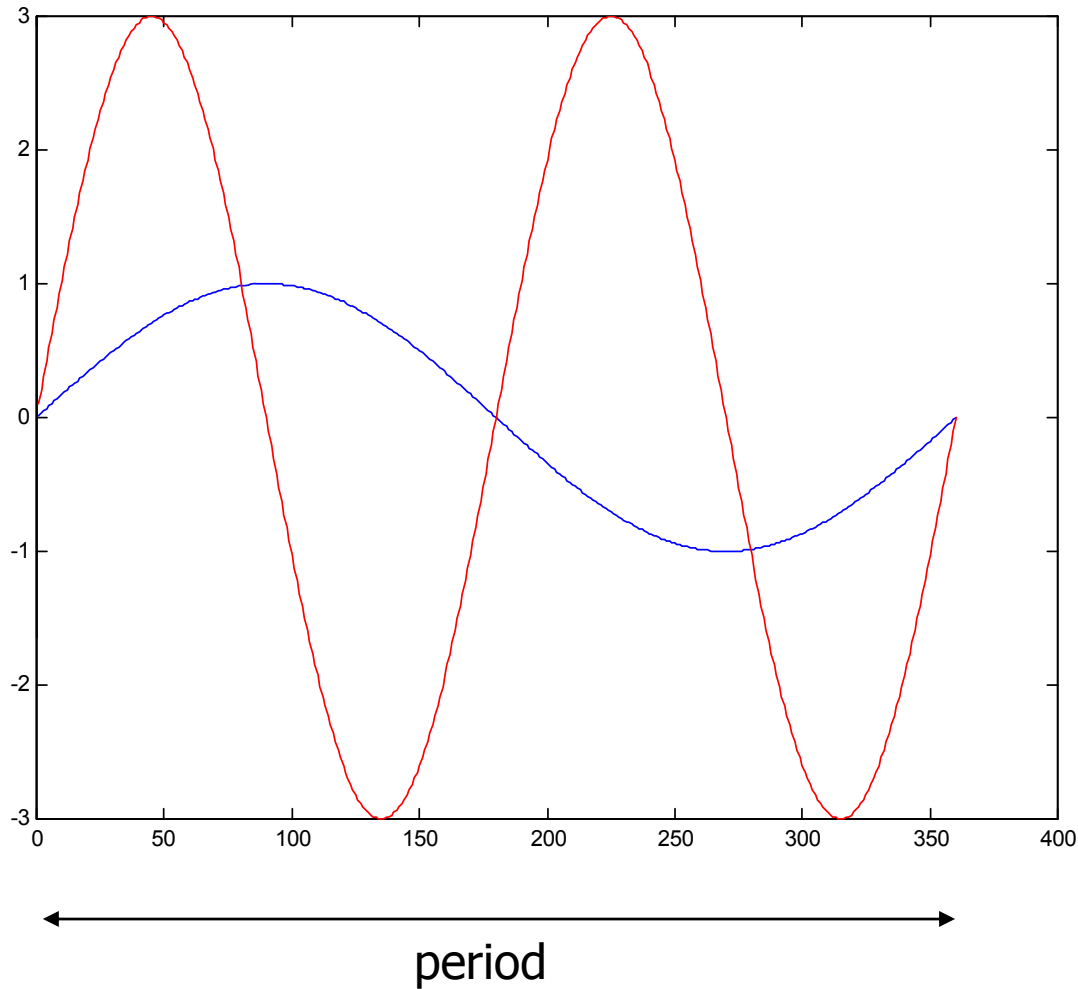
$1 * \sin(2x)$

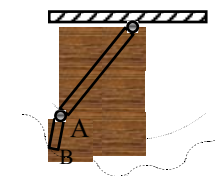




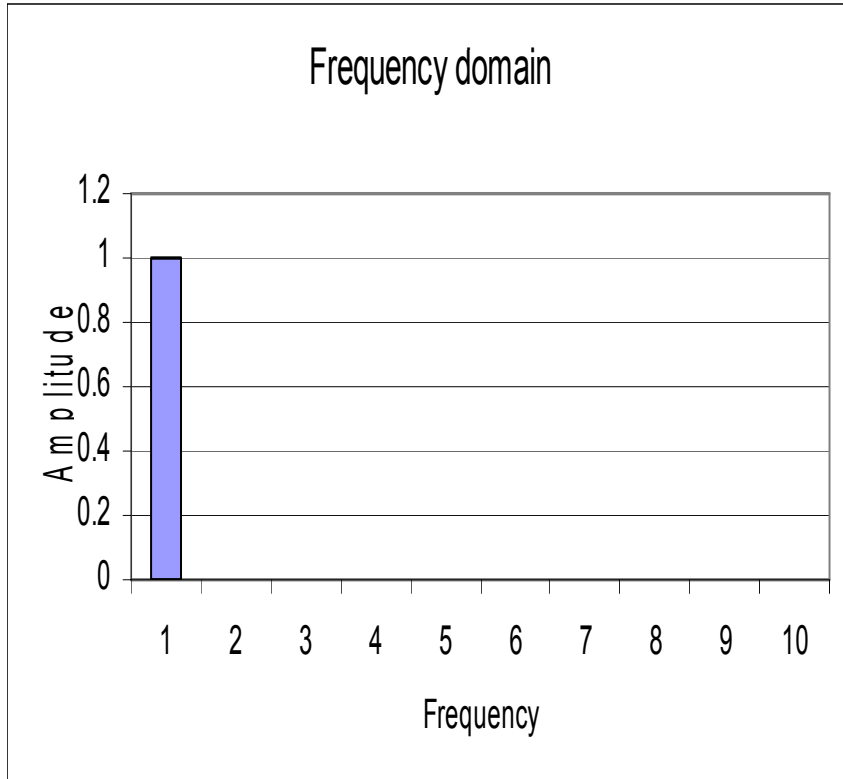
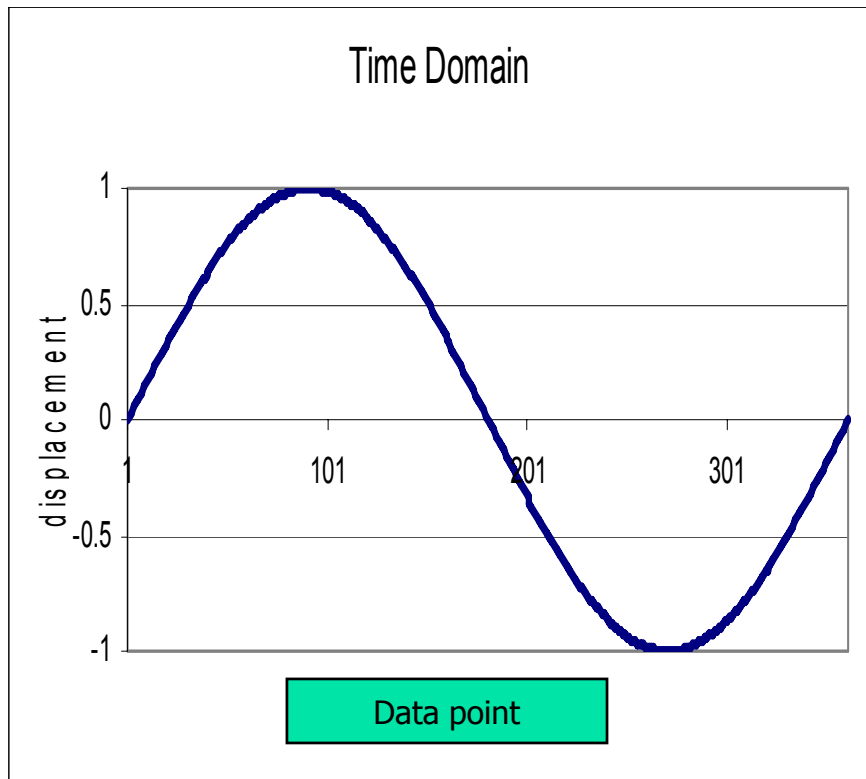
$\text{Sin}(x)$

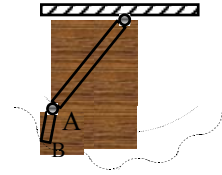
$3*\text{Sin}(2x)$



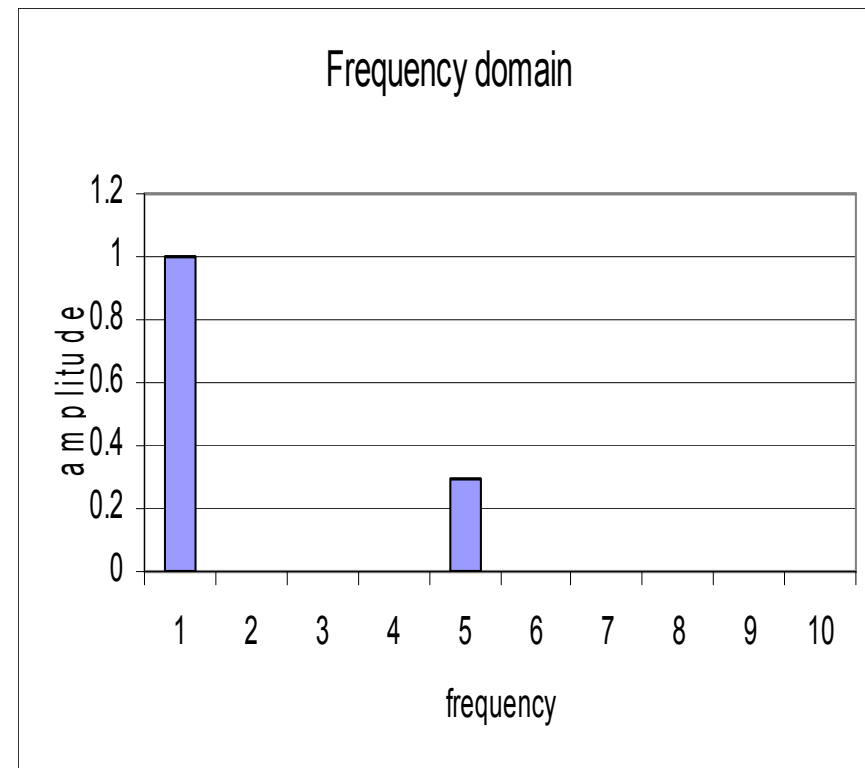
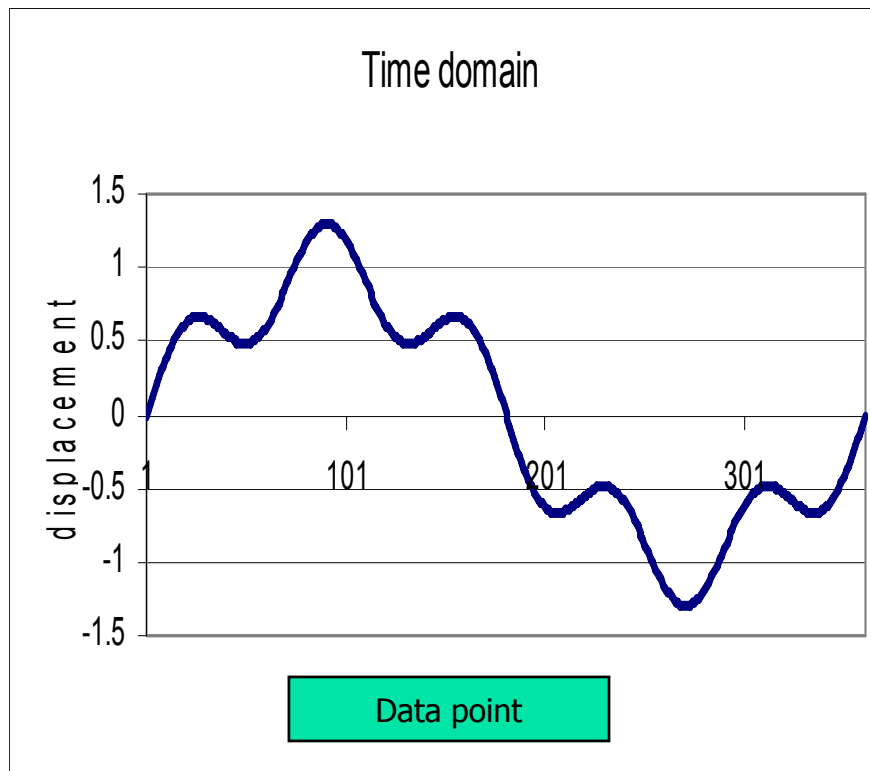


Time domain - Frequency domain



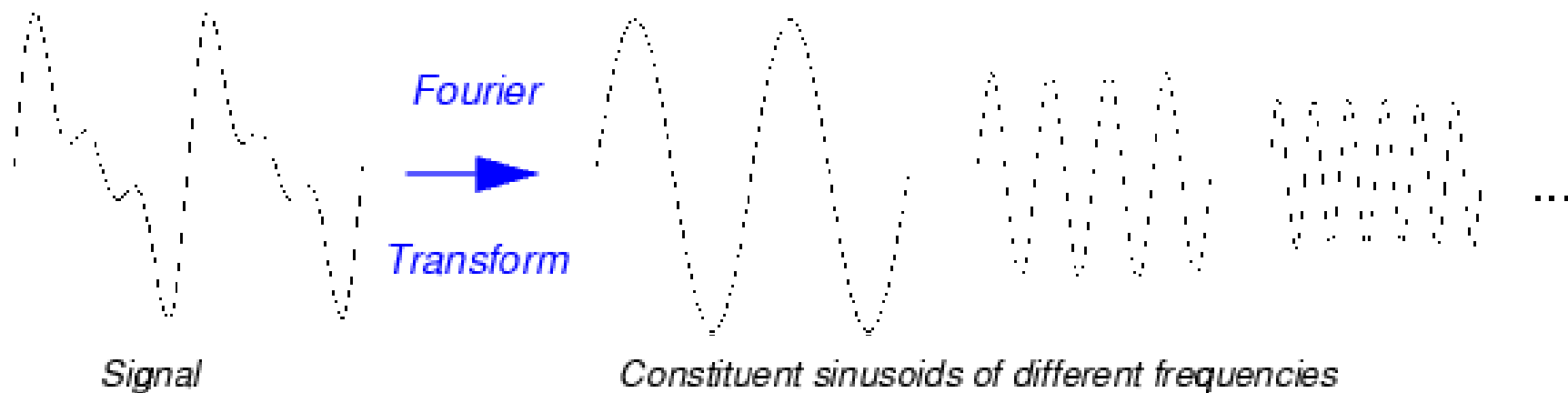


Time domain - Frequency domain

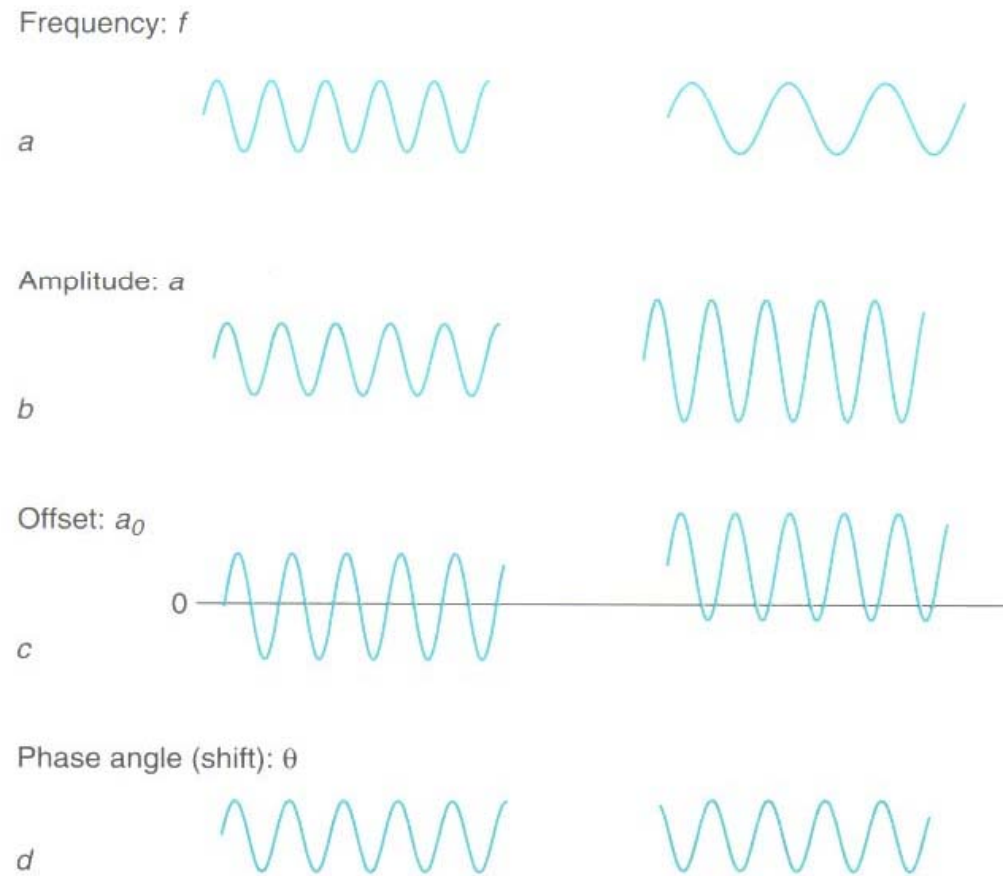


Time domain - frequency domain (Fourier Transform)

$$\text{Signal} = \sum [a \text{Sin}x + b \text{Cos}x] + c$$



Four essential components of time-varying signal



• **Figure 11.2** The four essential components of a time-varying signal.



Higher derivatives

- Velocity and acceleration
- Any error included in the displacement data will significantly be amplified via the differentiation process (ill posed problem)



$$\text{Signal} = \Sigma[a\text{Sin}x + b\text{Cos}x] + c$$

$$\text{DER}(\text{Sin}a^*X) = a^*\text{Cosa}^*X$$

$$\text{DER}(\text{Cosa}^*X) = -a^*\text{Sina}^*X$$

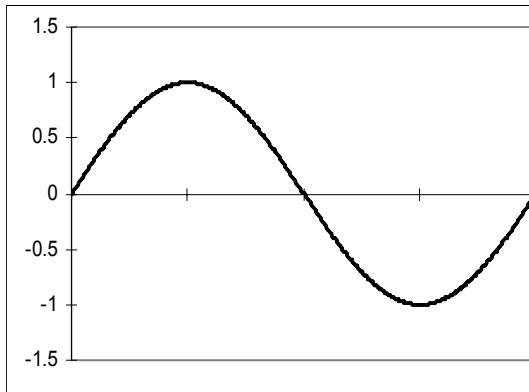
e.g.

$$\text{DER}(0.1^*\text{sin}(30^*X)) = 0.1^*30^*\text{Sin}(30^*X)$$

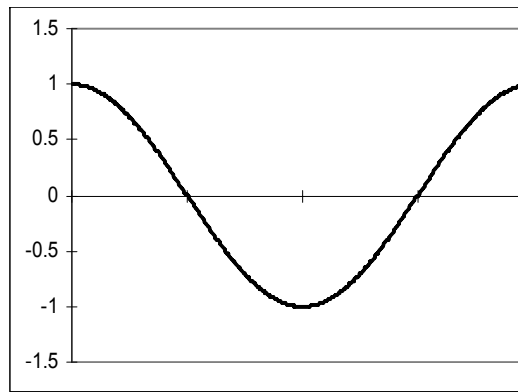


Higher derivatives

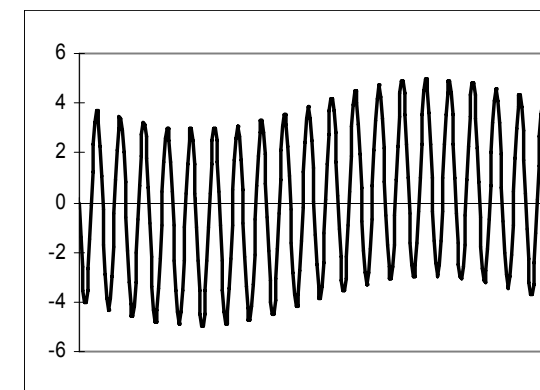
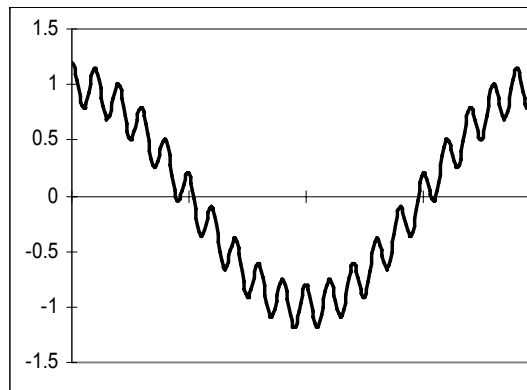
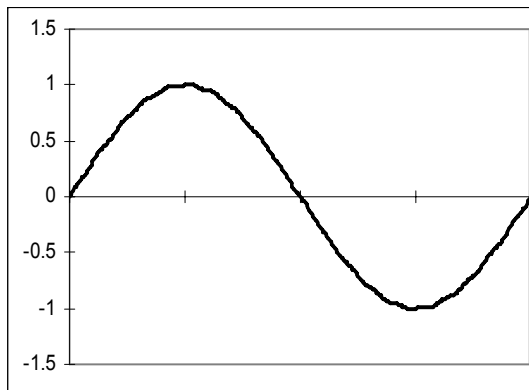
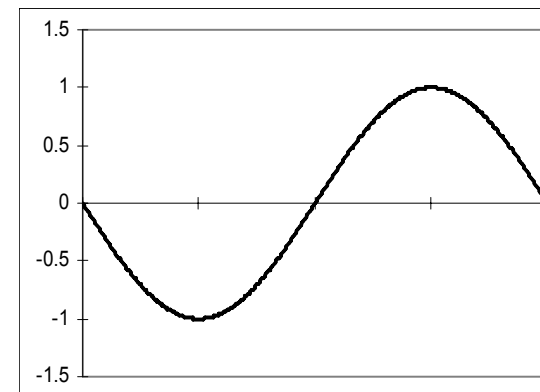
Displacement



Velocity

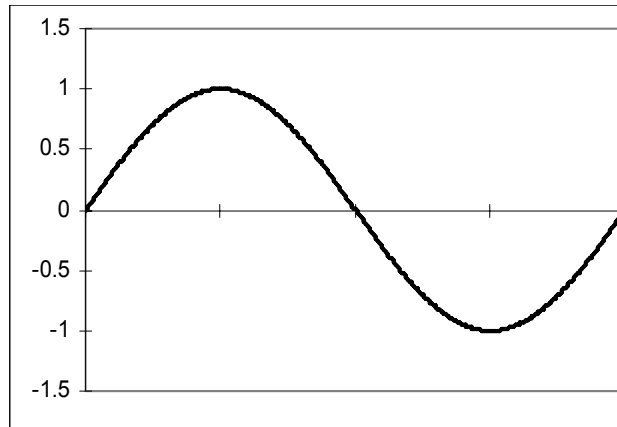


Acceleration

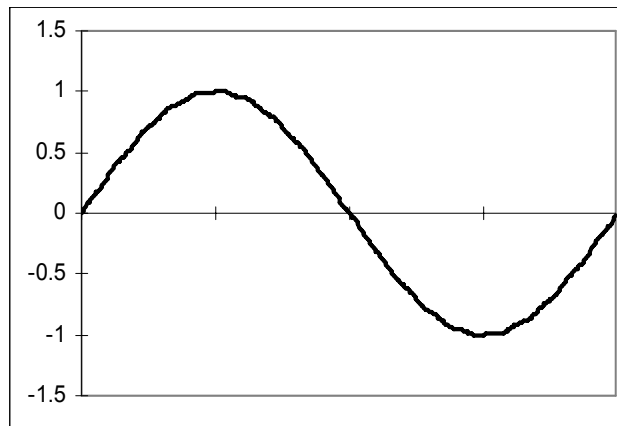
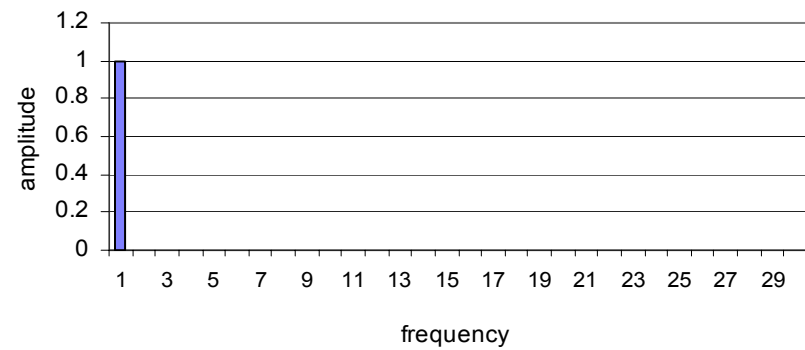


Displacement

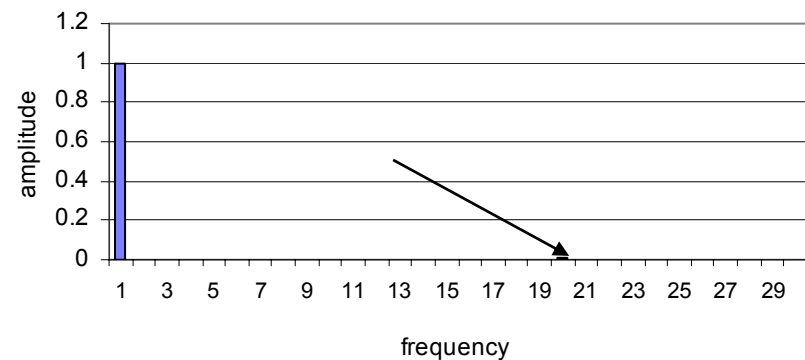
Clean signal



frequency domain



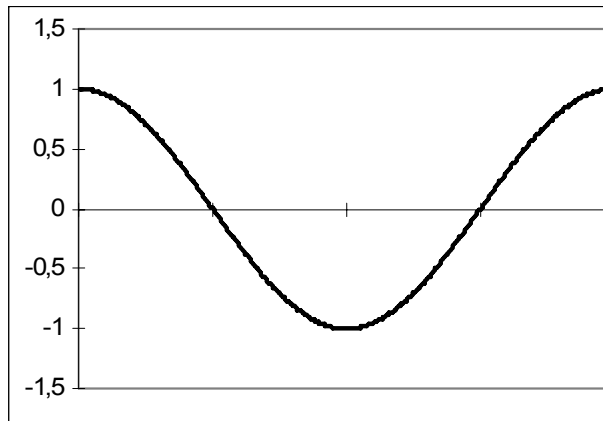
frequency domain



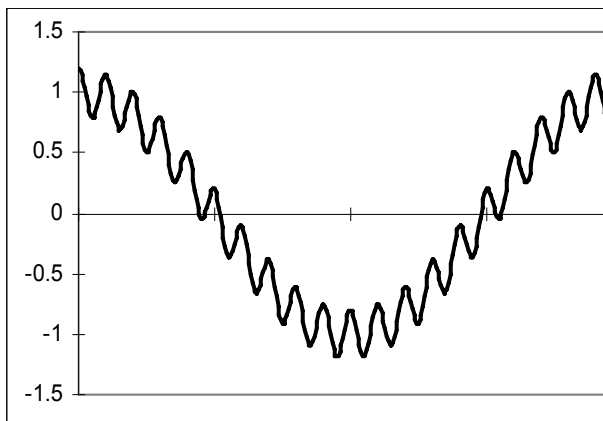
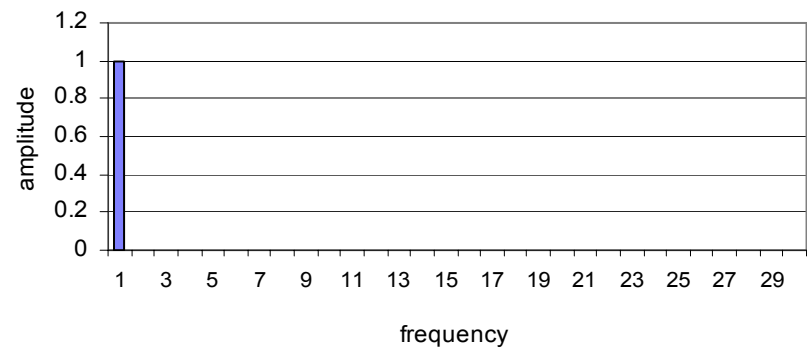
Noisy signal

Velocity

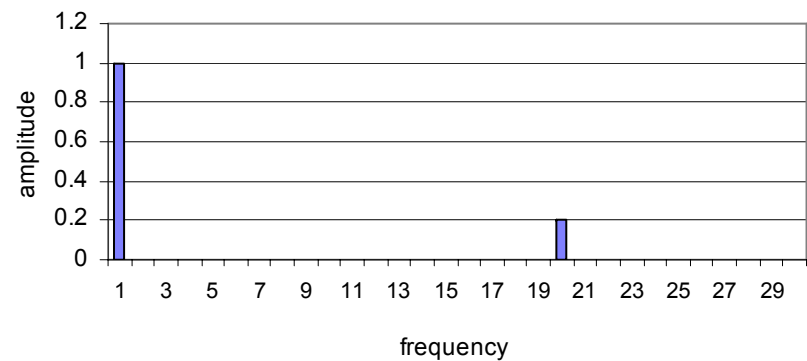
Clean signal



frequency domain



frequency domain

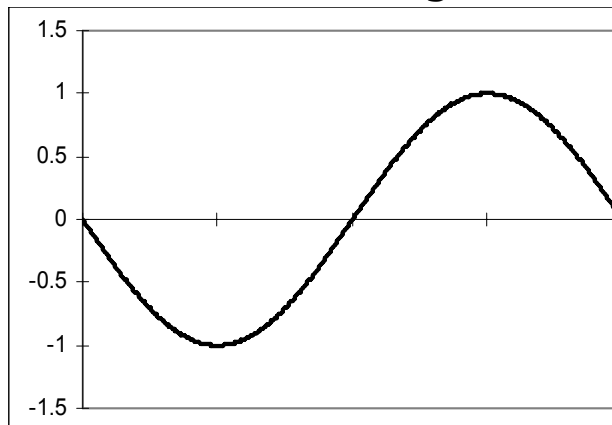


Noisy signal

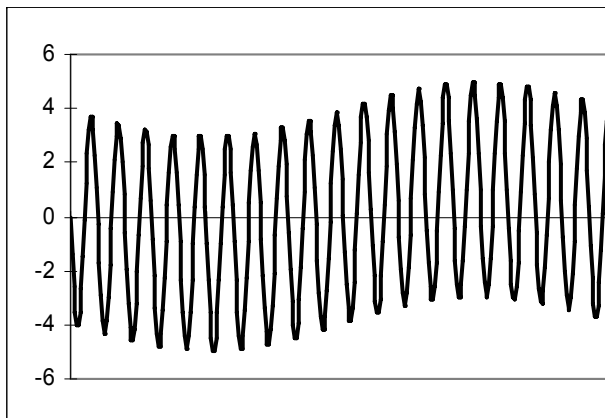
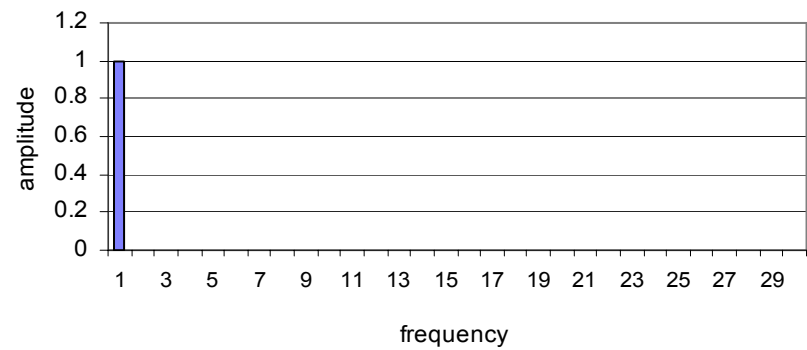
Data reproduced by Hatze (1990)

Acceleration

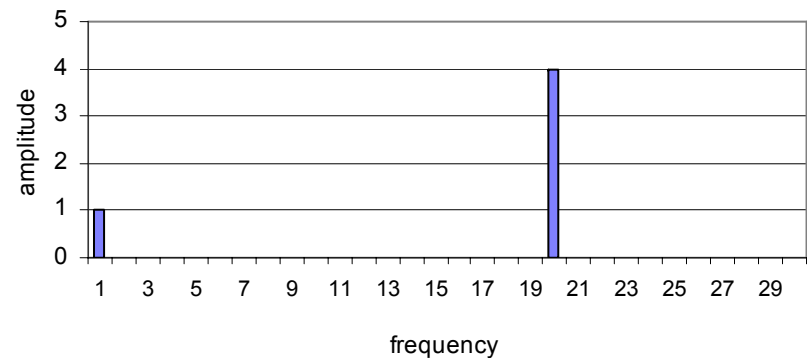
Clean signal



frequency domain



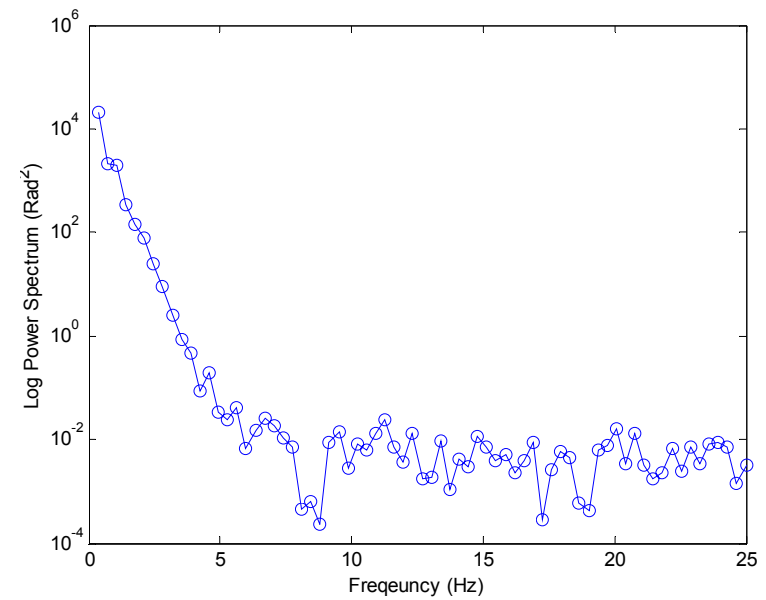
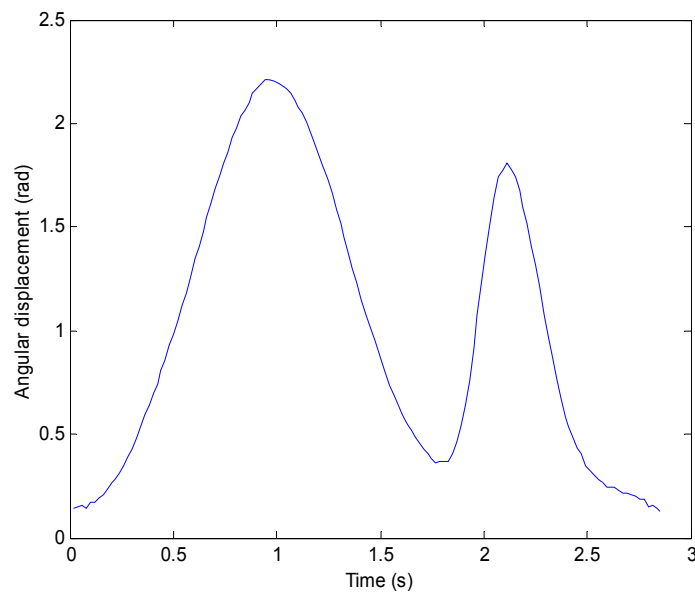
frequency domain



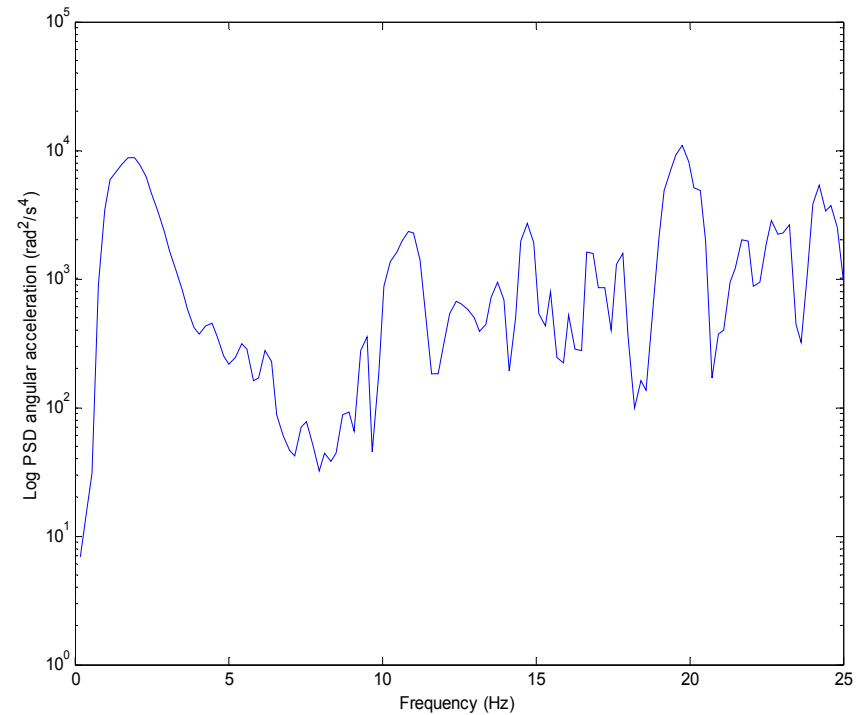
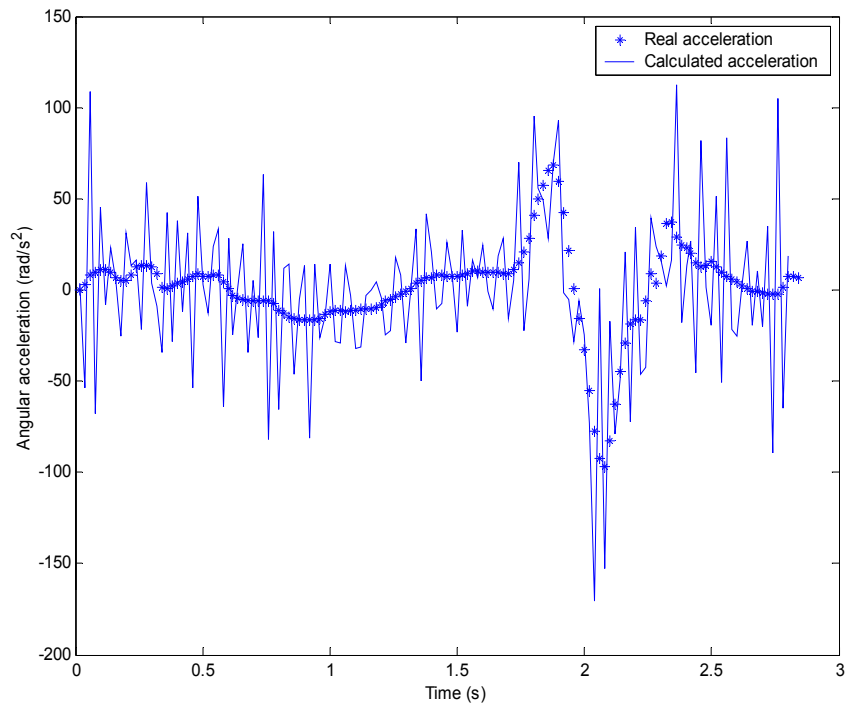
Noisy signal

Data reproduced by Hatze (1990)

Angular displacement of the elbow



Angular acceleration of the elbow



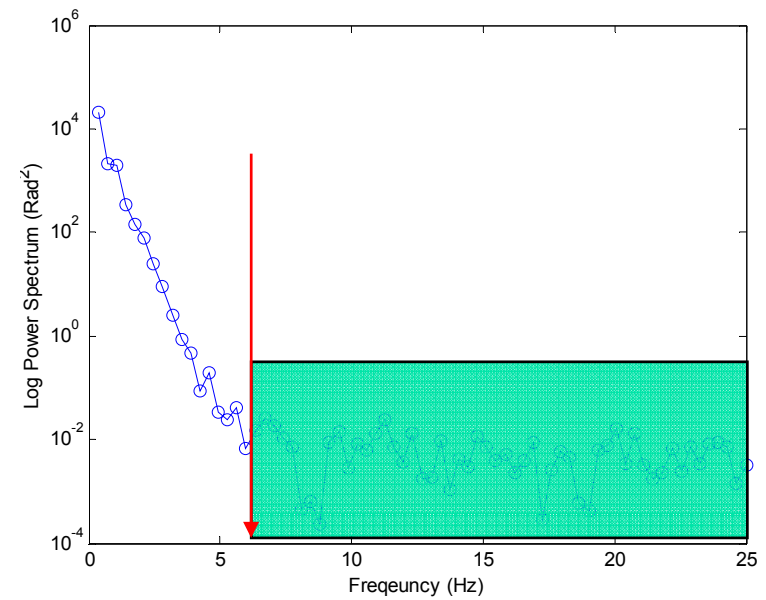
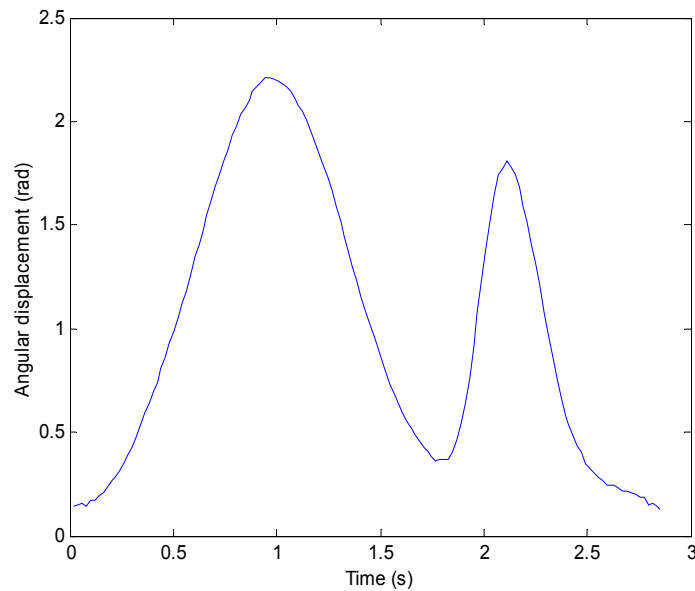


Problems

- Selection of appropriate cut-off frequency
- Differentiation process
- Endpoint distortion

- Signals are **non-stationary**

Angular displacement of the elbow





Selection of cut-off

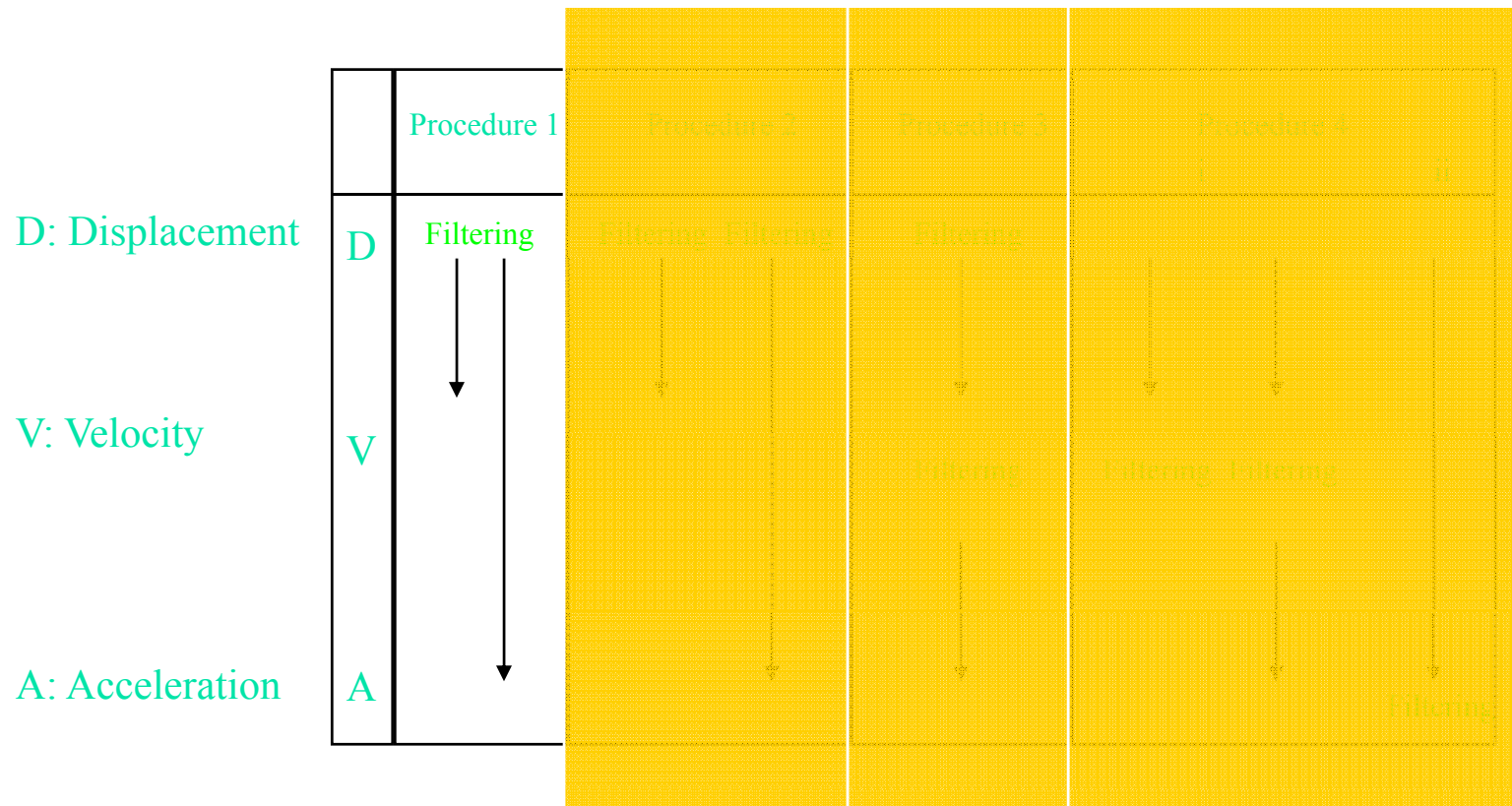
- Winter (1974)
- Hatze (1981)
- Woltring (1986)
- Dohrmann et al (1988)
- Damico and Ferrigno (1990)
- Simons and Yang (1991)
- Giakas and Baltzopoulos (1997a)
- Yu (1999)
- Challis (1999)
- Georgakis, Stergioulas and Giakas (2003)



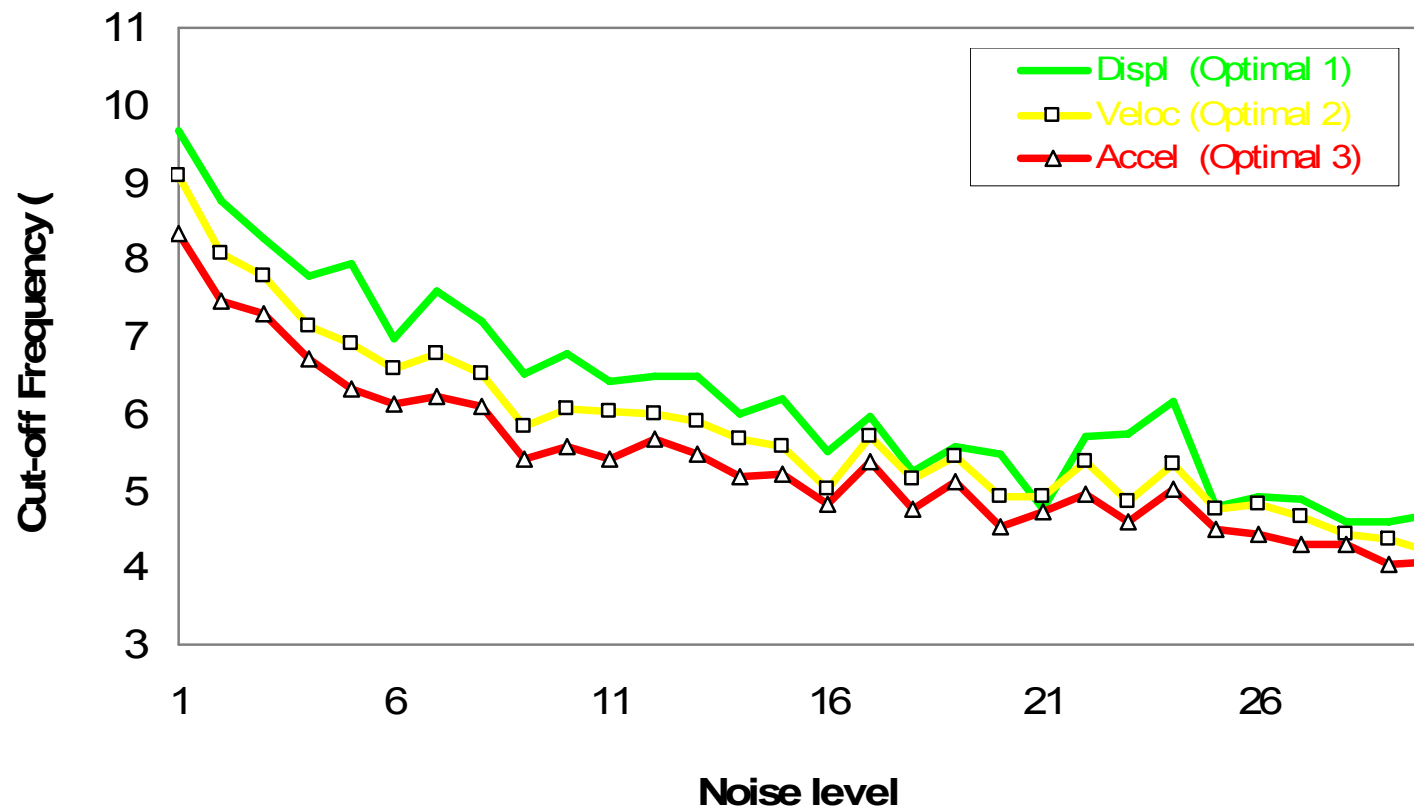
Differentiation process

- The calculation of velocity and acceleration requires a different cut-off frequency applied to the displacement data (Hatze, 1981; Giakas and Baltzopoulos, 1997b)

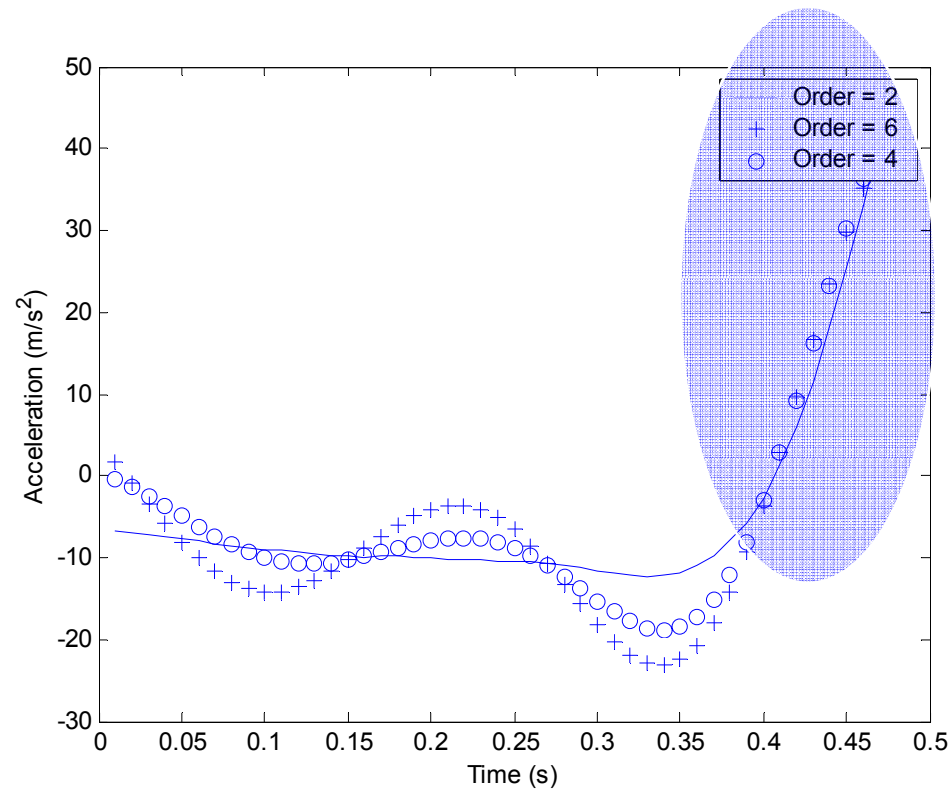
Differentiation process



Differentiation process



Endpoint distortion



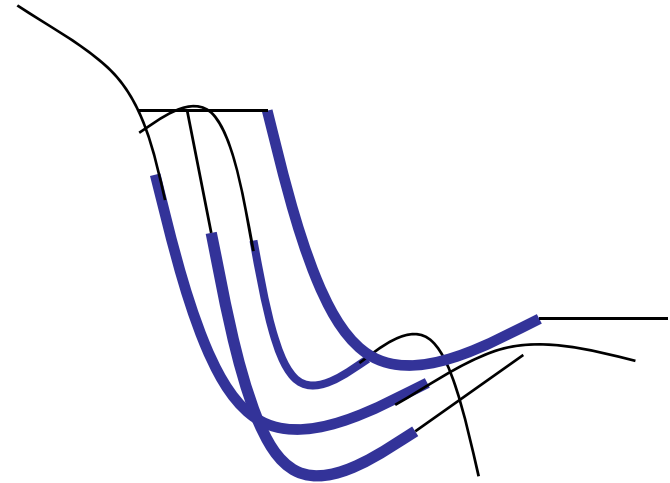
The signal is distorted at the edges when some filters are used



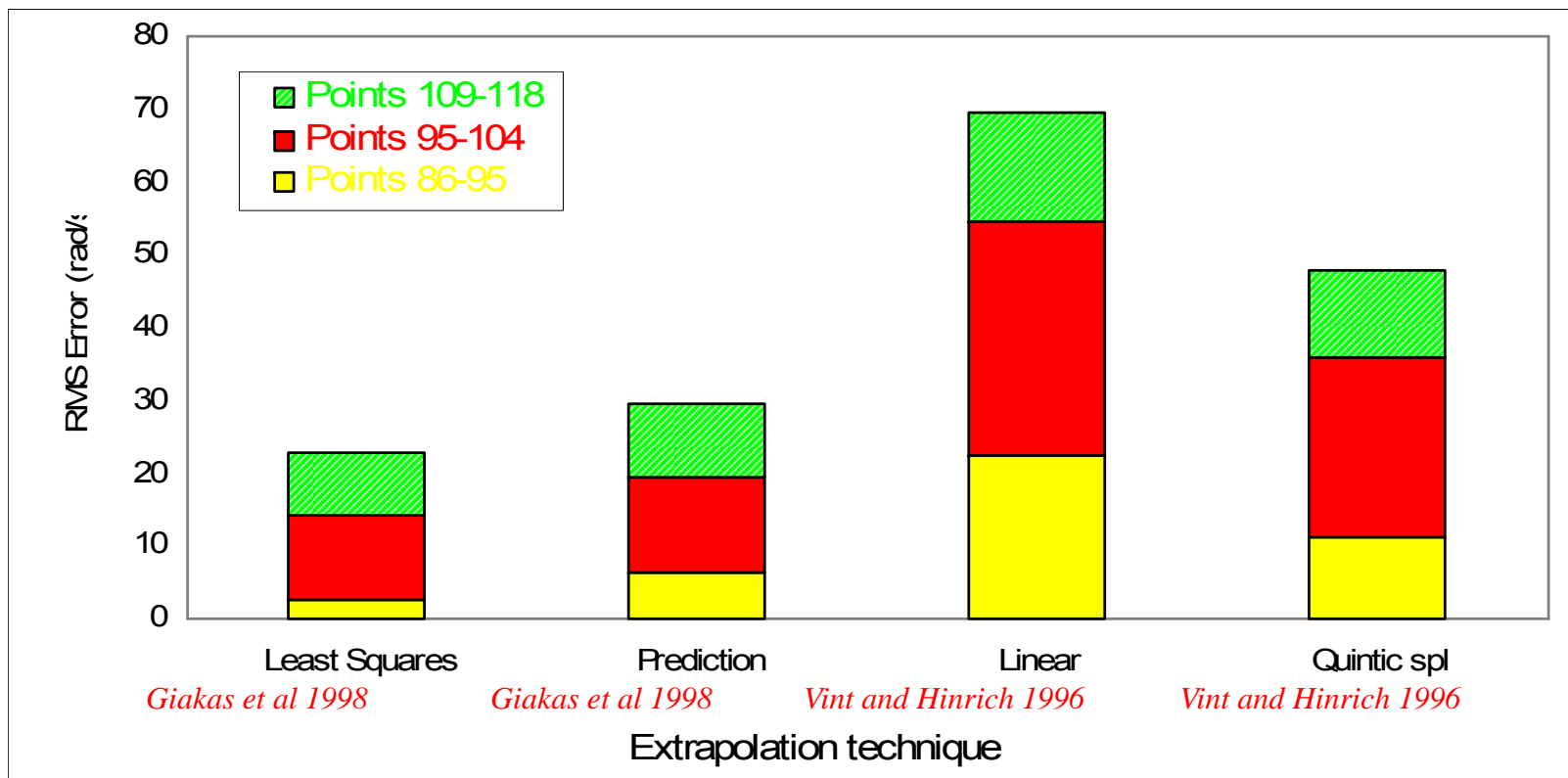


Endpoint distortion

- Smith (1989)
- Vint and Hinrichs (1996)
- Giakas et al (1998)



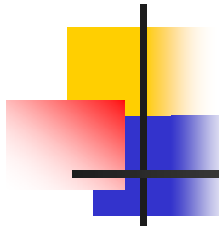
Endpoint distortion





Fundamentals

- Every single point requires a different cut-off frequency
- Every axis (of the same point) requires a different cut-off frequency
- Different data collection settings require adjustment of the filtering parameters



ggpsa502

File Help

D:\Giannis\Programs\MatLab\newgui\
DANCE1.3D

Sampling frequency (Hz) 100

ALL markers show TD
 save data show FD

R.FOOT 1

K< < > >>I

X 6.589 Y 7.364 Z 6.976
Cut-off Frequency (Hz)

Parameters

X Y Z Same X-Y-Z

Filter type Butterworth

Filter order 2

Number of poles 15

Noise above % 70

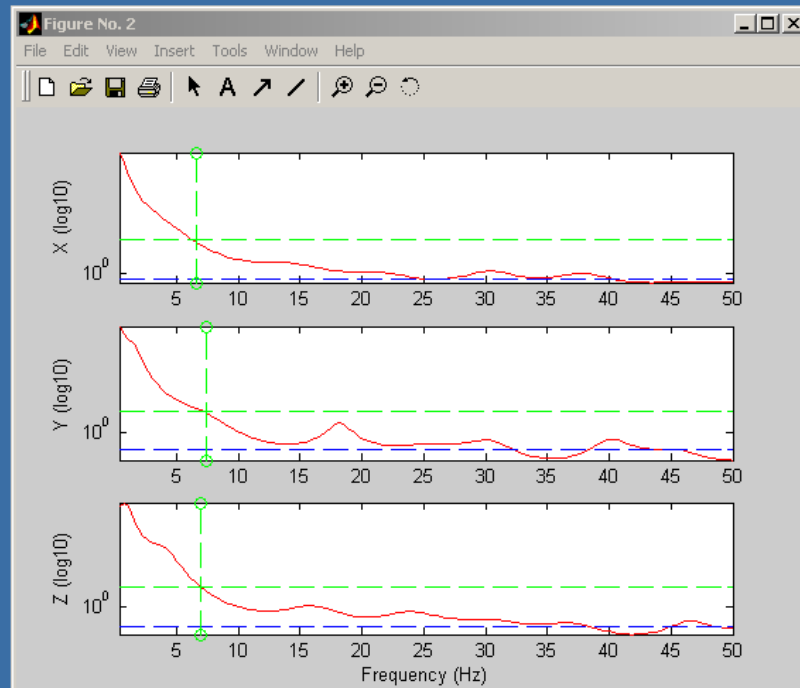
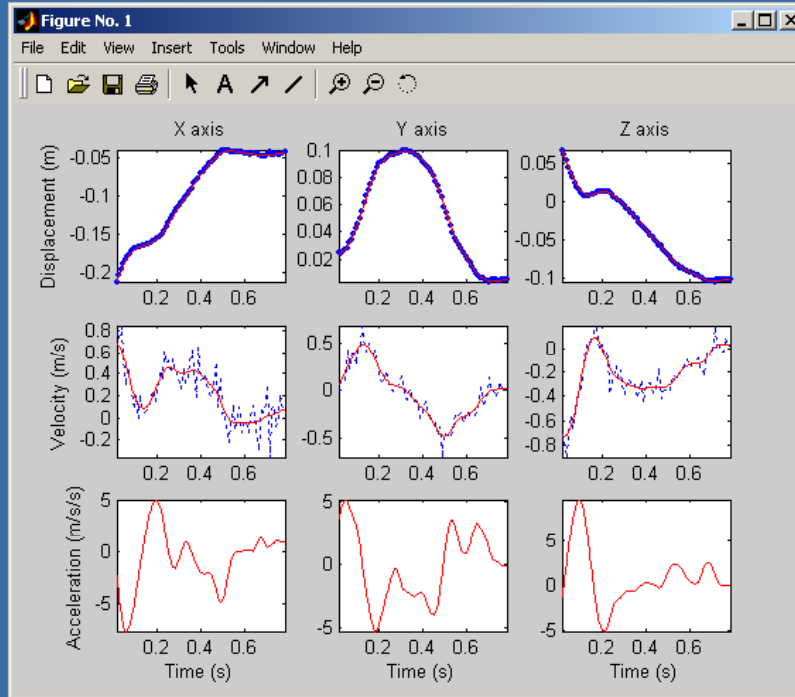
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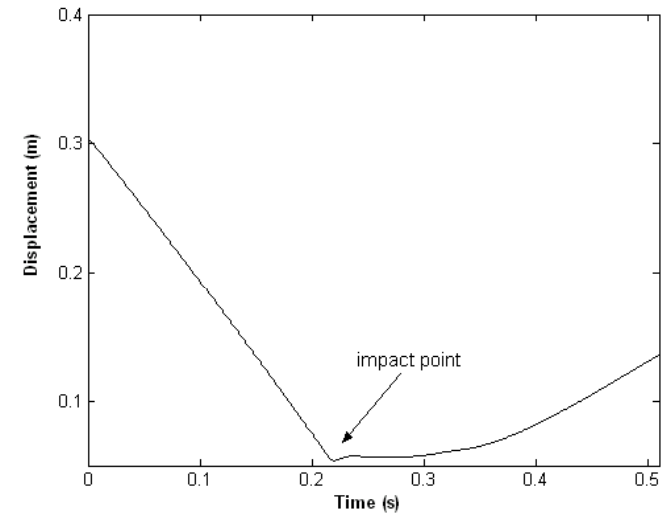
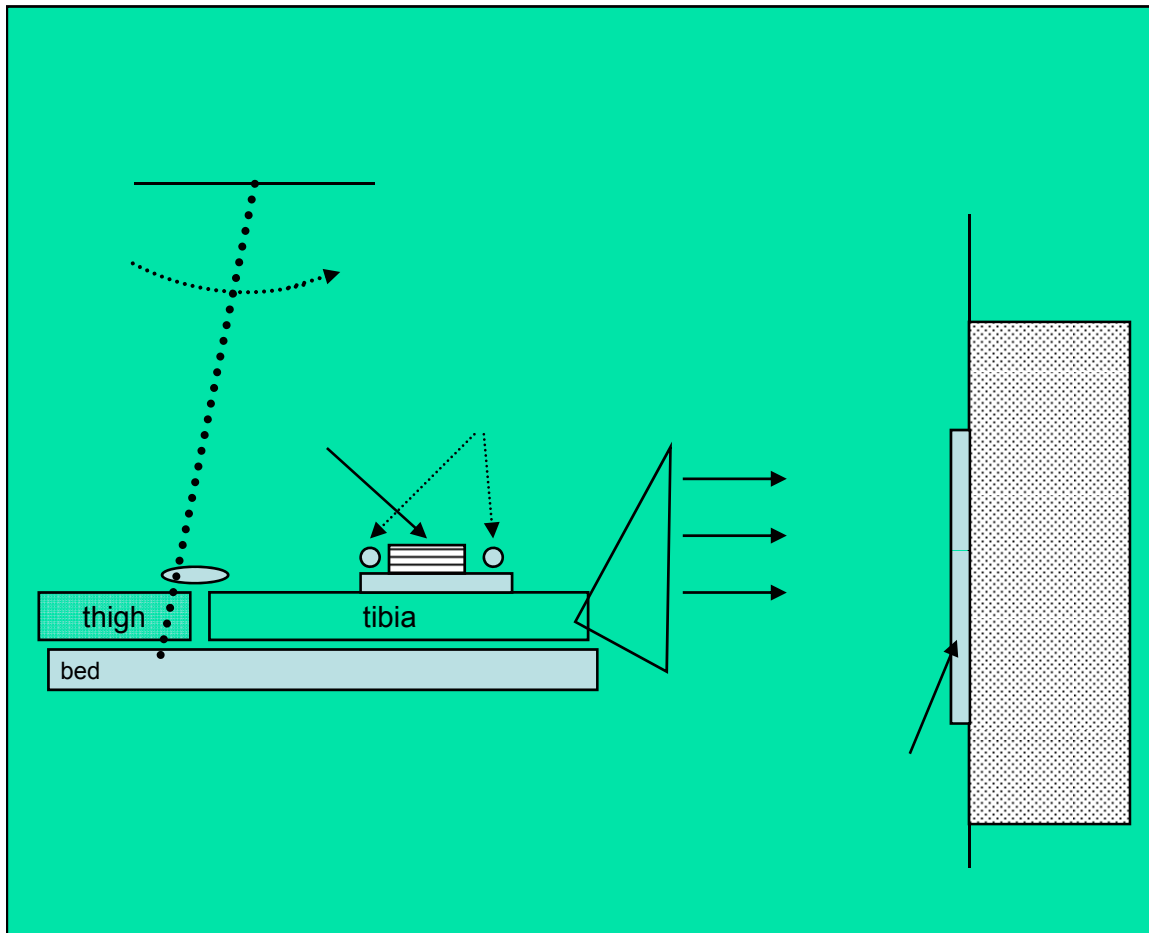
Extrapolation type Prediction

Extrapolated data 10

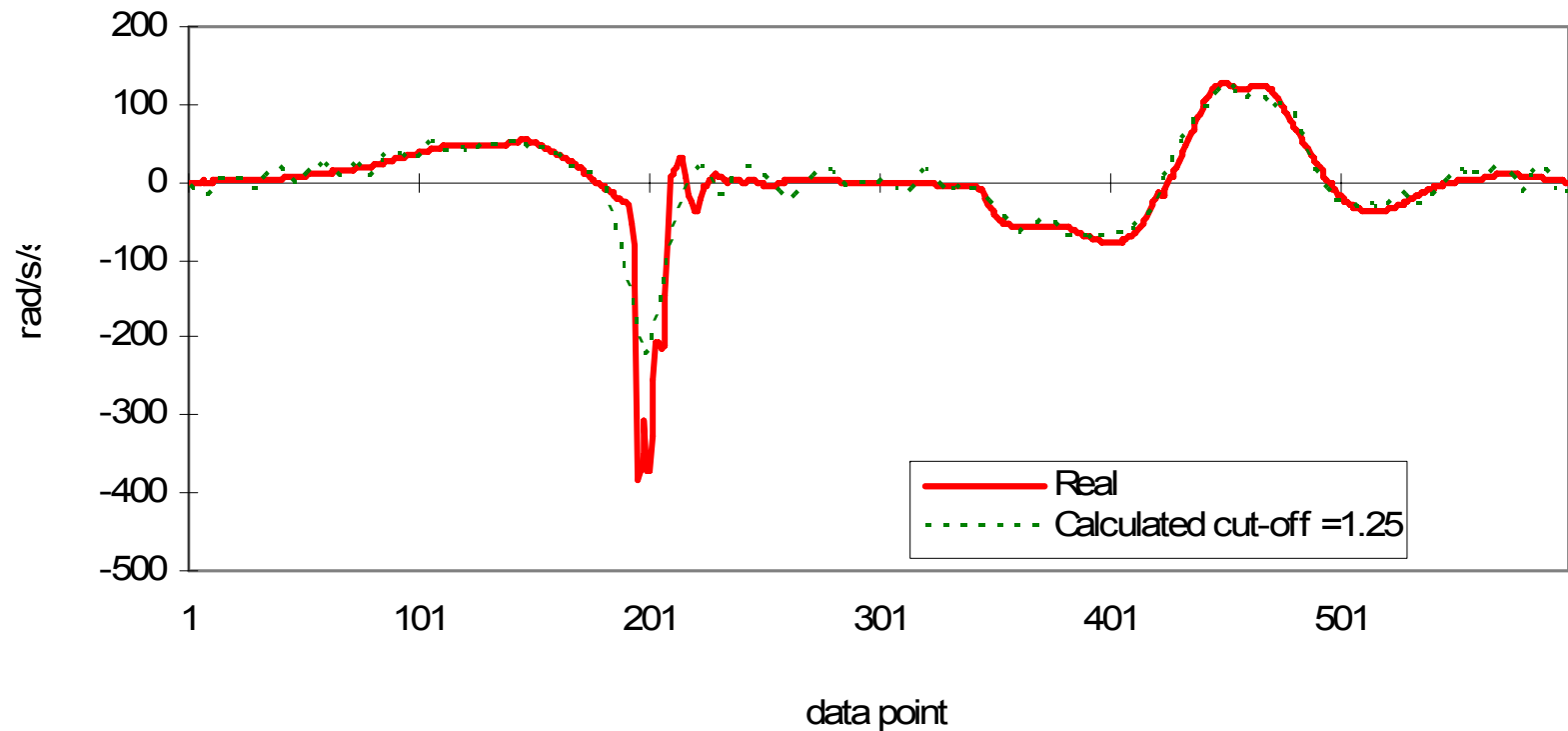
Undersampling 1

markers 19 frames 79

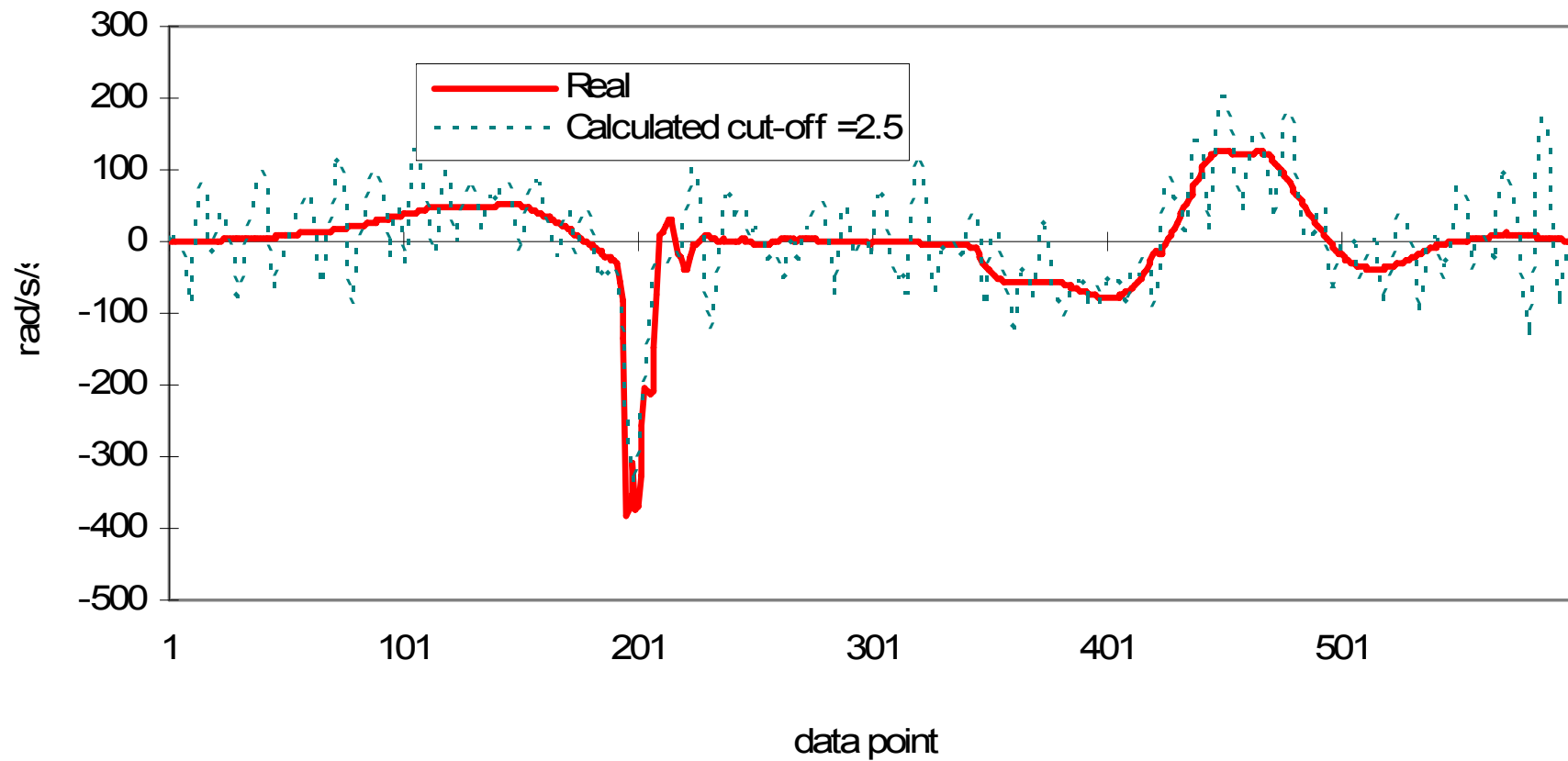


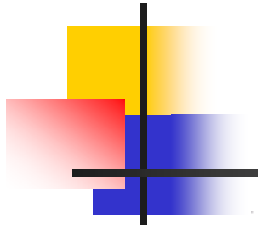


Signals are non stationary

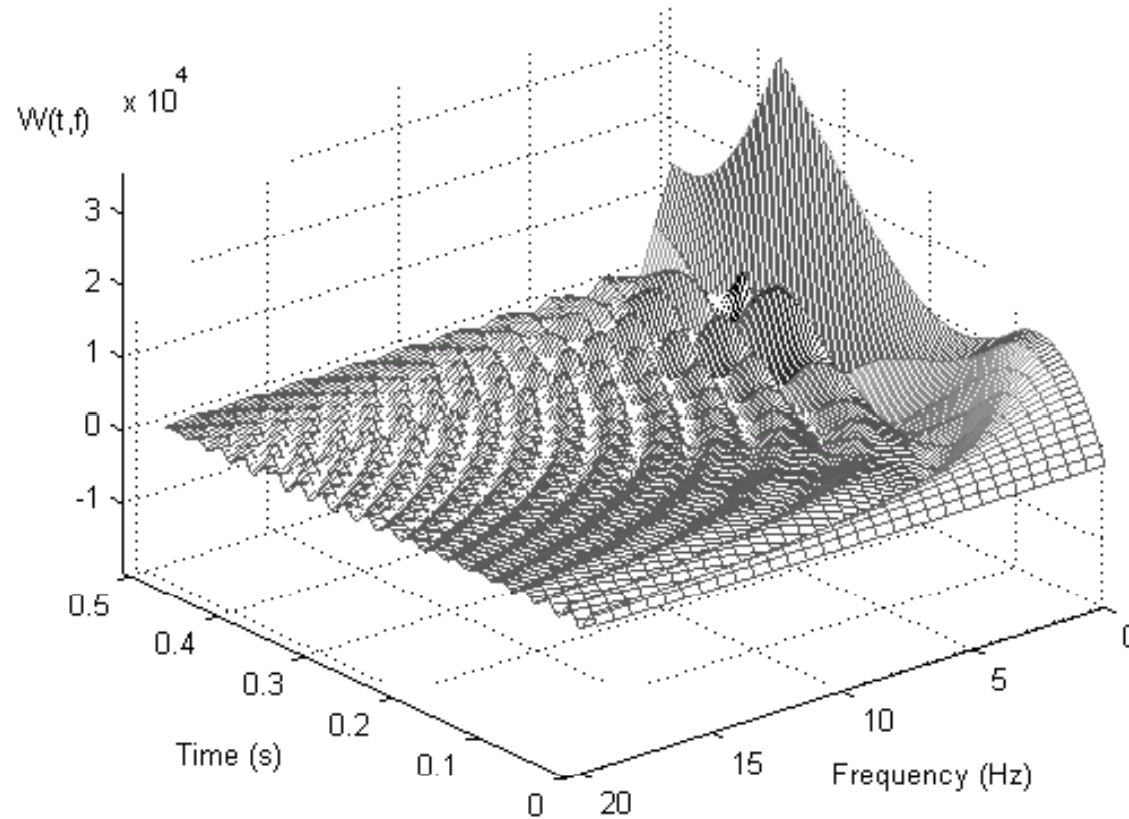


Signals are non stationary

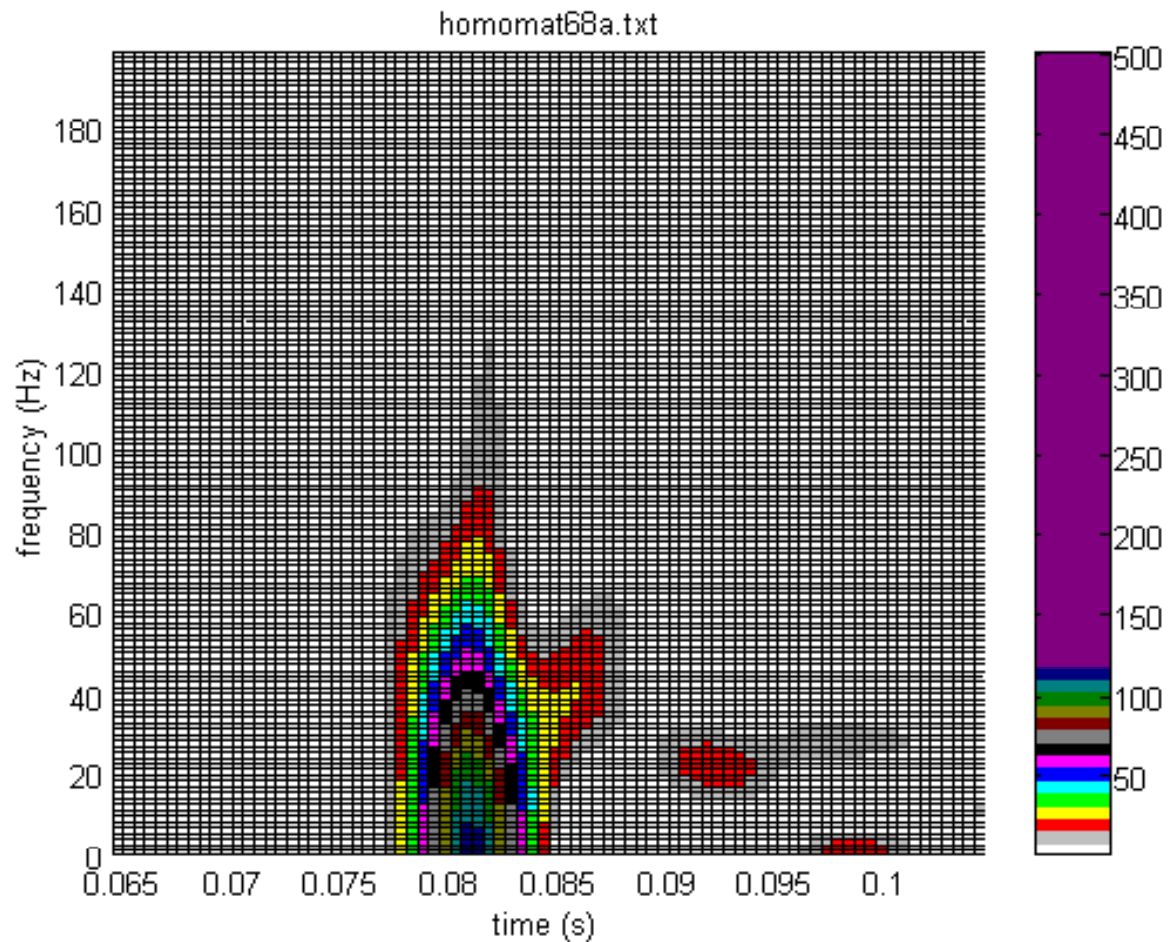




Joint time frequency analysis



Signals are non stationary





References

- **Giakas G** (2004). *Power Spectrum analysis and Filtering (Chapter 9)*. In N Stergiou (2004), *Innovative analyses of human movement. Human Kinetics, Champaign IL*.
- *Derrick T* (2004). *Signal Processing (Chapter 9)*. In Robertson et al (2004), *Research Methods in Biomechanics. Human Kinetics, Champaign IL*.
- Georgakis A, LK Stergioulas, and **G Giakas** (2003). An automatic algorithm for filtering kinematic signals with impacts in the Wigner representation. *Med & Biolog Eng & Comp* 40(6), 625-633.
- Georgakis A, LK Stergioulas, and **G Giakas** (2003). Fatigue analysis of the surface EMG signal in isometric constant force contractions using the averaged instantaneous frequency. *IEEE Transactions in Biomedical Engineering* 50(2), 262-265.
- Georgakis A, LK Stergioulas, and **G Giakas** (2002). Wigner filtering with smooth roll-off boundary for differentiation of noisy non-stationary signals. *Signal Processing* 82(10), 1411-1415.
- **Giakas G**, Vourdas A and LK Stergioulas (2000). A time-frequency domain approach for filtering non stationary kinematic signals. *J Biomechanics* 33, 567-574
- **Giakas G**, V Baltzopoulos and R M Bartlett (1998). Improved extrapolation techniques in recursive digital filtering: a comparison of least squares and prediction. *J Biomechanics* 31, 87-91
- **Giakas G** and V Baltzopoulos (1997a). A comparison of automatic filtering techniques applied to biomechanical walking data. *J Biomechanics* 30(8), 847-850
- **Giakas G** and V Baltzopoulos (1997b). Optimal digital filtering requires a different cut-off frequency strategy for the determination of the higher derivatives. *J Biomechanics* 30(8), 851-855